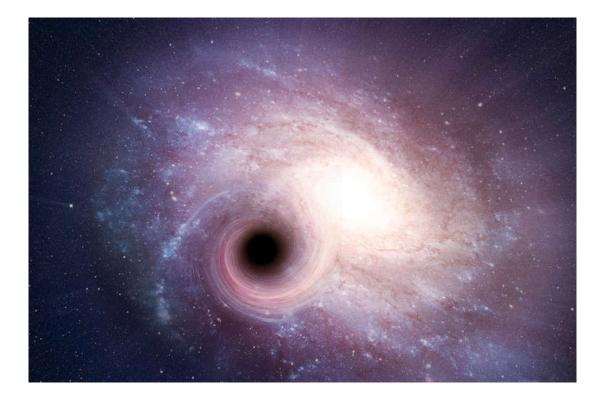
Analyzing some Ramanujan formulas: mathematical connections with various equations concerning some sectors of Black Hole Physics II

Michele Nardelli<sup>1</sup>, Antonio Nardelli

### Abstract

The purpose of this paper is to show how using certain mathematical values and / or constants from the Ramanujan expressions, we obtain some mathematical connections with equations of various sectors of Black Hole Physics

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Monster black hole 100,000 times more massive than the sun is found in the heart of

our galaxy (SMBH Sagittarius A = 1,9891\*10<sup>35</sup>) https://www.seeker.com/space/astronomy/new-class-of-black-hole-100000-times-larger-than-the-sundetected-in-milky-way



(N.O.A – Pics. from the web)

### From:

### A Reissner-Nordstrom+A black hole in the Friedman-Robertson-Walker

universe- arXiv:1703.05119v1 [physics.gen-ph] 5 Mar 2017

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Now, for

 $a(v) > \frac{\sqrt{k}}{4}$ . For the present universe, assuming a(v) = 1 and thus k < 16. Though constant k has an upper limit, it increases with the expansion of the universe and decreases with the contraction of the universe. We should observe a peculiar change when the constant k reaches this numerical value which is the limiting value for the expansion of the universe.

For Q = 0 in eqn.(64),

$$2(2 - \frac{\sqrt{1 + \frac{kx^2}{4}}}{ax})\left[\frac{M^2}{(\frac{ax}{\sqrt{1 + \frac{kx^2}{4}}})^3} - \frac{Q^2}{(\frac{ax}{\sqrt{1 + \frac{kx^2}{4}}})^3} + \Lambda e^{-\frac{2ax}{\sqrt{1 + \frac{kx^2}{4}}}}\right] + \frac{\sqrt{1 + \frac{kx^2}{4}}}{ax} = 0. \quad (64)$$

Hence at x = R we get,

$$2(2 - \frac{\sqrt{1 + \frac{kR^2}{4}}}{aR}) \left[ \frac{M^2}{(\frac{aR}{\sqrt{1 + \frac{kR^2}{4}}})^3} - \frac{Q^2}{(\frac{aR}{\sqrt{1 + \frac{kR^2}{4}}})^3} + \Lambda e^{-\frac{2aR}{\sqrt{1 + \frac{kR^2}{4}}}} \right] + \frac{\sqrt{1 + \frac{kR^2}{4}}}{aR} - 0.$$
(65)

$$\Lambda = -e^{\frac{2aR}{\sqrt{1+\frac{kR^2}{4}}}} \cdot \left[\frac{M^2}{(\frac{aR}{\sqrt{1+\frac{kR^2}{4}}})^3} + \frac{1}{2(\frac{2aR}{\sqrt{1+\frac{kR^2}{4}}} - 1)}\right],$$
(67)

For k = 12, and a = 1, M = 13.12806e+39; R = 1.94973e+13, we obtain:

and:

(1+((12\*(1.94973e+13)^2)/4))^1/2

### Input interpretation:

 $\sqrt{1+\frac{1}{4}\left(12\left(1.94973\times10^{13}\right)^{2}\right)}$ 

**Result:** 3.37703... × 10<sup>13</sup> 3.37703e+13

Substituting in the eqs. (67), we obtain:

 $-\exp(((2*1.94973e+13)/(3.37703e+13))) * [(((13.12806e+39)^{2})) / (((1.94973e+13)/(3.37703e+13)))^{3} + 1/((2((((2*1.94973e+13)/(3.37703e+13)-1)))))]$ 

### Input interpretation:

$$- \exp \Biggl( \frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}} \Biggr) \Biggl( \frac{(13.12806 \times 10^{39})^2}{\left(\frac{1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right)^3} + \frac{1}{2 \left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}} - 1\right)} \Biggr)$$

### **Result:**

 $-2.84160... \times 10^{81}$ 

-2.84160...\*10<sup>81</sup> which represents the Cosmological Constant inside the Schwarzschild black hole and also has a negative value.

From the previous expression, we have also that:

### **Input interpretation:**

$$\begin{split} &\log \left(-\exp\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right) \left(\frac{\left(13.12806 \times 10^{39}\right)^2}{\left(\frac{1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right)^3} + \frac{1}{2\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}} - 1\right)}\right)\right) - \\ & 47 - \frac{1}{4} - \frac{1}{\phi} \end{split}$$

log(x) is the natural logarithm  $\phi$  is the golden ratio

### **Result:**

139.686... + 3.14159... i

### **Polar coordinates:**

r = 139.721 (radius),  $\theta = 1.28839^{\circ}$  (angle) 139.721 result practically equal to the rest mass of Pion meson 139.57 MeV

### Input interpretation:

$$\log \left( -\exp\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right) \left(\frac{\left(13.12806 \times 10^{39}\right)^2}{\left(\frac{1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right)^3} + \frac{1}{2\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}} - 1\right)} \right) \right) - 55 - 8 + \frac{1}{\phi}$$

 $\log(x)$  is the natural logarithm  $\phi$  is the golden ratio

### **Result:**

125.172... + 3.14159... i

### **Polar coordinates:**

r = 125.211 (radius),  $\theta = 1.43772^{\circ}$  (angle) 125.211 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

### **Input interpretation:**

$$27 \times \frac{1}{2} \left( \log \left( -\exp\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right) \left(\frac{(13.12806 \times 10^{39})^2}{\left(\frac{1.94973 \times 10^{13}}{3.37703 \times 10^{13}}\right)^3} + \frac{1}{2\left(\frac{2 \times 1.94973 \times 10^{13}}{3.37703 \times 10^{13}} - 1\right)} \right) \right) - 55 - 5 + \frac{1}{\phi} \right) - 1.618034$$

log(x) is the natural logarithm  $\phi$  is the golden ratio

### **Result:**

1728.70... + 42.4115... i

### **Polar coordinates:**

r = 1729.22 (radius),  $\theta = 1.4054^{\circ}$  (angle) 1729.22

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

### From Wikipedia:

"The fundamental group of the complex form, compact real form, or any algebraic version of  $E_6$  is the cyclic group  $\mathbb{Z}/3\mathbb{Z}$ , and its outer automorphism group is the cyclic group  $\mathbb{Z}/2\mathbb{Z}$ . Its fundamental representation is 27-dimensional (complex), and a basis is given by the 27 lines on a cubic surface. The dual representation, which is inequivalent, is also 27-dimensional. In particle physics,  $E_6$  plays a role in some grand unified theories".

From

$$16\pi p(r) = -16\pi \rho(r) = \frac{2Q^2}{r^4} - \frac{M}{r^3} + \frac{4\Lambda}{3},$$
(30)

For M = 13.12806e+39; R= r = 1.94973e+13; Q = 0.00089 and  $\Lambda = -1.1056 * 10^{-46}$ 

We obtain:

$$16\pi p(r) = -16\pi \rho(r) = \frac{2Q^2}{r^4} - \frac{M}{r^3} + \frac{4\Lambda}{3}, \qquad (30)$$

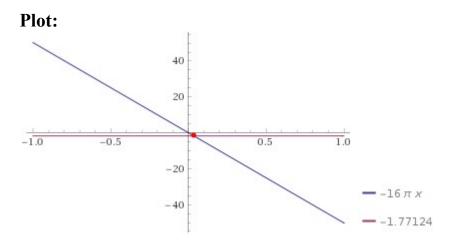
 $-16Pi^*x = \frac{2*0.00089^2}{(1.94973e+13)^4} - \frac{13.12806e+39}{(1.94973e+13)^3} + \frac{(4*(-1.1056e-46))}{3}$ 

### Input interpretation:

 $-16\,\pi\,x = \frac{2 \times 0.00089^2}{\left(1.94973 \times 10^{13}\right)^4} - \frac{13.12806 \times 10^{39}}{\left(1.94973 \times 10^{13}\right)^3} + \frac{1}{3}\left(4\left(-1.1056 \times 10^{-46}\right)\right)$ 

### **Result:**

 $-16 \pi x = -1.77124$ 



Alternate form:  $1.77124 - 16 \pi x = 0$ 

### Solution:

 $x \approx 0.0352377$ 

0.0352377

Indeed, we have:

-16Pi\*(0.0352377)

### Input interpretation:

 $-16 \pi \times 0.0352377$ 

### **Result:**

-1.77123999119041691518360141995181022051959353830976266220... -1.77123999119...

 $\frac{(2*0.00089^{2})}{(1.94973e+13)^{4}} - \frac{(13.12806e+39)}{(1.94973e+13)^{3}} + \frac{(4*(-1.1056e+46))}{3}$ 

### **Result:**

 $-1.77123885495274173001001460199604480791346216969960288749\ldots$ 

-1.7712388549...

### We have also:

 $\frac{1+1}{(-(((((2*0.00089^{2})/(1.94973e+13)^{4} - (13.12806e+39)/(1.94973e+13)^{3} + (4*(-1.1056e-46))/3)))^{11}}{(4*(-1.1056e-46))^{3})))^{11}}$ 

### **Input interpretation:**

 $1 + -\frac{1}{\left(\frac{2 \times 0.00089^2}{\left(1.94973 \times 10^{13}\right)^4} - \frac{13.12806 \times 10^{39}}{\left(1.94973 \times 10^{13}\right)^3} + \frac{1}{3}\left(4\left(-1.1056 \times 10^{-46}\right)\right)\right)^{11}}$ 

### **Result:**

1.001857597267683517285996862255287161325131442715831071767...

1.00185759726768.....result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{2\pi}{5}}}{\sqrt{\varphi\sqrt{5}} - \varphi} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}} \approx 1.0018674362$$

and:

 $\begin{array}{l} [1/(((((1+1/(-(((((2*0.00089^{2})/(1.94973e+13)^{4} - (13.12806e+39)/(1.94973e+13)^{3} + (4*(-1.1056e-46))/3))))^{1/3} \end{array}$ 

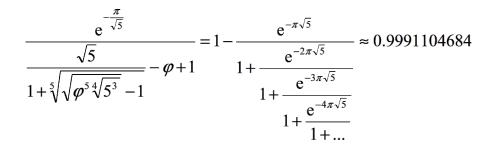
### Input interpretation:

$$\sqrt[3]{\frac{1}{\left(\frac{2\times0.00089^2}{\left(1.94973\times10^{13}\right)^4}-\frac{13.12806\times10^{39}}{\left(1.94973\times10^{13}\right)^3}+\frac{1}{3}\left(4\left(-1.1056\times10^{-46}\right)\right)}\right)^{11}}$$

### **Result:**

0.9993816...

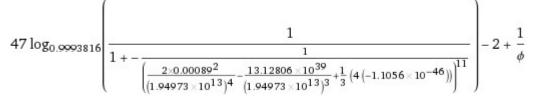
0.9993816... result very near to the value of the following Rogers-Ramanujan continued fraction:



and to the dilaton value **0**. **989117352243** =  $\phi$ 

 $\begin{array}{l} 47*\log base \ 0.9993816[1/(((((1+1/(-(((((2*0.00089^2)/(1.94973e+13)^4 - (13.12806e+39)/(1.94973e+13)^3 + (4*(-1.1056e-46))/3))))^{-11})))))]-2+1/golden \\ ratio \end{array}$ 

### **Input interpretation:**



 $\log_b(x)$  is the base- b logarithm  $\phi$  is the golden ratio

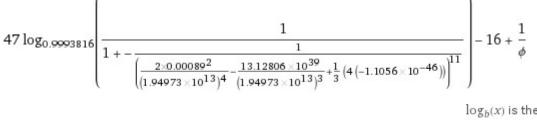
### **Result:**

139.626...

139.626... result practically equal to the rest mass of Pion meson 139.57 MeV

47\*log base  $0.9993816[1/(((((1+1/(-(((((2*0.00089^2)/(1.94973e+13)^4 - (13.12806e+39)/(1.94973e+13)^3 + (4*(-1.1056e-46))/3))))^{11}))))]-16+1/golden ratio$ 

### **Input interpretation:**



 $\log_b(x)$  is the base- b logarithm  $\phi$  is the golden ratio

### **Result:**

125.626...

125.626... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

From:

$$\nu' = \frac{2}{\left(1 - \frac{2M}{r} + \frac{Q^2}{r^2} - \frac{\Lambda r^2}{3}\right)} \cdot \left(\frac{M}{r^2} - \frac{Q^2}{r^3} - \frac{\Lambda r}{3}\right), \quad (37)$$

For M = 13.12806e+39; R = r = 1.94973e+13; Q = 0.00089 and

 $\Lambda = -1.1056 * 10^{-46}$ 

 $2/[((1-((2*13.12806e+39)/(1.94973e+13))+((0.00089^{2})/(1.94973e+13)^{2})-(1/3((-1.1056e-46)*(1.94973e+13)^{2}))))]$ 

### **Input interpretation:**

 $\frac{2}{1-\frac{2\times13.12806\times10^{39}}{1.94973\times10^{13}}+\frac{0.00089^2}{\left(1.94973\times10^{13}\right)^2}-\frac{1}{3}\left(-1.1056\times10^{-46}\left(1.94973\times10^{13}\right)^2\right)}$ 

### **Result:**

 $-1.485162316442795051210917684294429459965147476183849...\times10^{-27}\\-1.485162316\ldots*10^{-27}$ 

 $((13.12806e+39)/(1.94973e+13)^{2})-((0.00089^{2})/(1.94973e+13)^{3})-(((1/3(-1.1056e-46)*(1.94973e+13)))))$ 

### **Input interpretation:**

 $\frac{13.12806 \times 10^{39}}{(1.94973 \times 10^{13})^2} - \frac{0.00089^2}{(1.94973 \times 10^{13})^3} - \frac{1}{3} \left(-1.1056 \times 10^{-46}\right) \times 1.94973 \times 10^{13}$ 

### **Result:**

 $\begin{array}{l} 3.4534375326670091332524257699497484433331145959128445...\times10^{13}\\ 3.45343753266\ldots\ast10^{13} \end{array}$ 

### Thence:

2/[((1-((2\*13.12806e+39)/(1.94973e+13))+((0.00089^2)/(1.94973e+13)^2)-(1/3((-1.1056e-46)\*(1.94973e+13)^2))))]\*3.453437532667009133252425769949748443333114595 9128445 × 10^13

### Input interpretation:

 $\frac{2}{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{0.00089^2}{(1.94973 \times 10^{13})^2} - \frac{1}{3} \left(-1.1056 \times 10^{-46} \left(1.94973 \times 10^{13}\right)^2\right)} \times 10^{10}$ 

 $3.4534375326670091332524257699497484433331145959128445 \times 10^{13}$ 

### **Result:**

 $-5.128915285706225990265318791538218923755584238005614... \times 10^{-14}$ 

 $-5.12891528570622599...*10^{-14}$ 

From which:

**Input interpretation:** 

$$\left( - \left( \frac{1}{2} \left( \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{0.00089^2}{(1.94973 \times 10^{13})^2} - \frac{1}{3} \left( -1.1056 \times 10^{-46} \left( 1.94973 \times 10^{13} \right)^2 \right) \right) \times 3.45343753266700913 \times 10^{13} \right) \right) \uparrow (1/6) - 24 - \frac{1}{\phi}$$

 $\phi$  is the golden ratio

### **Result:**

139.439...

139.439... result practically equal to the rest mass of Pion meson 139.57 MeV

Input interpretation:  $\left(-\left(1/\left(2/\left(1-\frac{2\times13.12806\times10^{39}}{1.94973\times10^{13}}+\frac{0.00089^2}{(1.94973\times10^{13})^2}-\frac{1}{3}\left(-1.1056\times10^{-46}\left(1.94973\times10^{13}\right)^2\right)\right)\times\right)$ 3.45343753266700913×10<sup>13</sup>)))  $(1/6) - 34 - 4 - \frac{1}{\phi}$ 

 $\phi$  is the golden ratio

### **Result:**

125.439...

125.439... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV 27\*1/2((((([-1/(((((2/[((1-((2\*13.12806e+39)/(1.94973e+13))+((0.00089^2)/(1.94973e+13)^2)-(1/3((-1.1056e-46)\*(1.94973e+13)^2))))]\*3.45343753266700913e+13))))))]^1/6-34-golden ratio)))))-5

### **Input interpretation:**

$$27 \times \frac{1}{2} \left( \left( -\left( \frac{1}{2} \right) \left( \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{0.00089^2}{(1.94973 \times 10^{13})^2} - \frac{1}{3} \left( -1.1056 \times 10^{-46} \left( 1.94973 \times 10^{13} \right)^2 \right) \right) \times 3.45343753266700913 \times 10^{13} \right) \right) \right) \land (1/6) - 34 - \phi \right) - 5$$

 $\phi$  is the golden ratio

### **Result:**

1728.93... 1728.93... ≈ 1729

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

(((27\*1/2((((([-1/((((((2/[((1-((2\*13.12806e+39)/(1.94973e+13))+((0.00089^2)/(1.94973e+13)^2)-(1/3((-1.1056e-46)\*(1.94973e+13)^2))))]\*3.4534375326e+13))))))]^1/6-34-golden ratio)))))-5)))^1/15 -0.16^2

### **Input interpretation:**

$$\left( 27 \times \frac{1}{2} \left( \left( -\left( 1 / \left( 2 / \left( 1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{0.00089^2}{(1.94973 \times 10^{13})^2} - \frac{1}{3} \left( -1.1056 \times 10^{-46} \left( 1.94973 \times 10^{13} \right)^2 \right) \right) \times 3.4534375326 \times 10^{13} \right) \right) \right)$$

$$(1/6) - 34 - \phi - 5 \right) (1/15) - 0.16^2$$

### **Result:**

1.618210857780689573829233821017956708451644304924909702237...

1.61821085778... result that is a very good approximation to the value of the golden ratio 1,618033988749...

From:

### Generating functions of wormholes

arXiv:1901.01757v1 [physics.gen-ph] 1 Jan 2019

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### Ksh. Newton Singh<sup>‡</sup>

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### Neeraj Pant<sup>§</sup>

Faculty of Computational Sciences, Department of Mathematics, National Defence Academy, Khadakwasla, Pune-411023, India. (Dated: January 8, 2019)

### We have that:

The form of the shape function  $b(r) = r_0 [1 + \beta^2 (1 - \frac{r_0}{r})]$ , where  $r_0$  is the throat radius, provides a wormhole solution provided the arbitrary constant  $\beta$  has the restriction  $\beta^2 < 1$  since  $b'(r_0) < 1$ .

Here the generating functions are

$$Z(r) = \frac{1}{r} \quad \text{and} \quad \Pi(r) = \frac{3\beta^2 r_0^2}{r^4} - \frac{2r_0(1+\beta^2)}{r^3}.$$
 (18)

The form  $8\pi(P_r + \rho)$  is given by

$$8\pi(P_r+\rho) = \frac{2\beta^2 r_0^2}{r^4} - \frac{r_0}{r^3} - \frac{\beta^2 r_0}{r^3}.$$
(19)

From:

$$Z(r) = \frac{1}{r}$$
$$\Pi(r) = \frac{3\beta^2 r_0^2}{r^4} - \frac{2r_0(1+\beta^2)}{r^3}.$$
$$\beta^2 < 1$$

we obtain:

1/(1.94973e+13)

# Input interpretation:

 $1.94973 imes 10^{13}$ 

### **Result:**

 $5.1289152857062259902653187877295830704764249408892513...\times 10^{-14}$ 

### **Repeating decimal:**

 $5.1289152857062259902653187877295830704764249408892513... \times 10^{-14}$ (period 10192)

5.12891528570622599...× 10<sup>-14</sup>

For r = 1.94973e+13 and  $\beta^2 = 0.5^2$ 

 $(3*0.5^{2}*x^{2})/(1.94973e+13)^{4} - (2*x(1+0.5^{2}))/(1.94973e+13) = y$ 

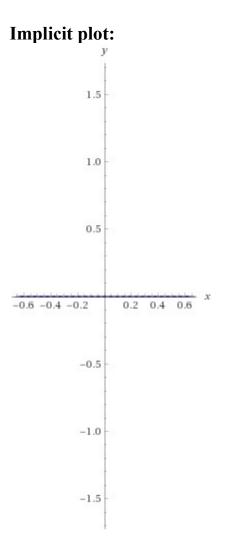
 $\frac{3 \times 0.5^2 x^2}{(1.94973 \times 10^{13})^4} - \frac{2 x (1 + 0.5^2)}{1.94973 \times 10^{13}} = y$ 

### **Result:**

 $5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x = y$ 

# **Geometric figure:**

line



## Alternate forms:

 $(5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x = y$ 

 $2.27815 \times 10^{-27} (2.27815 \times 10^{-27} x - 5.62839 \times 10^{13}) x = y$ 

 $5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x - y = 0$ 

Alternate form assuming x and y are real:  $5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x + 0 = y$ 

### **Real solution:**

 $y \approx 3.40721 \times 10^{-64} \; \big( 1.52323 \times 10^{10} \; x^2 - 3.76328 \times 10^{50} \; x \big)$ 

### Solution:

 $y \approx 3.40721 \times 10^{-64} x (15\,232\,265\,625\,x - 376\,328\,121\,043\,228\,610\,302\,385\,975\,708\,522\,214\,756\,492\,565\,807\,104)$ 

### **Integer solution:**

x = 0, y = 0

### **Partial derivatives:**

 $\frac{\partial}{\partial x} (5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x) = 1.03799 \times 10^{-53} x - 1.28223 \times 10^{-13}$  $\frac{\partial}{\partial y} (5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x) = 0$ 

### **Implicit derivatives:**

 $\frac{\partial x(y)}{\partial y} = 1467476454883228089433232610286553682370173274290168791040.00000/$ (-188164060521614286264410022193656773292990987763712+15232265625x) $<math display="block">\frac{\partial y(x)}{\partial x} = -\frac{1}{7798920000000} +$ 

*x* 96 339 998 987 066 514 567 377 931 363 152 267 926 011 385 735 020 544

### **Global minimum:**

 $\min\{5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x\} = -\frac{183753965353138951430087912298492942668936511488}{232021916070556640625} \text{ at} \\ x = \frac{188164060521614286264410022193656773292990987763712}{15232265625}$ 

 $(3*0.5^{2}x^{2})/(1.94973e+13)^{4} - (2*x(1+0.5^{2}))/(1.94973e+13) = (5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x$ 

# Input interpretation:

 $\frac{3 \times 0.5^2 x^2}{(1.94973 \times 10^{13})^4} - \frac{2 x (1 + 0.5^2)}{1.94973 \times 10^{13}} = (5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x$ 

### **Result:**

 $5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x = (5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x$ 

### **Alternate forms:**

 $2.30701 \times 10^{-60} x^2 + 1.17857 \times 10^{-19} x = 0$ 

 $(5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x = (5.18995 \times 10^{-54} x - 1.28223 \times 10^{-13}) x$ 

 $2.27815 \times 10^{-27} (2.27815 \times 10^{-27} x - 5.62839 \times 10^{13}) x =$  $2.27815 \times 10^{-27} (2.27815 \times 10^{-27} x - 5.62839 \times 10^{13}) x$ 

### **Expanded form:**

 $5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x = 5.18995 \times 10^{-54} x^2 - 1.28223 \times 10^{-13} x$ 

### Alternate form assuming x is real:

 $5.18995 \times 10^{-54} x^{2} - 1.28223 \times 10^{-13} x + 0 =$  $5.18995 \times 10^{-54} x^{2} - 1.28223 \times 10^{-13} x + 0$ 

### **Solutions:**

 $x = -51\,086\,681\,842\,193\,045\,893\,000\,894\,180\,192\,294\,010\,880$ 

x = 0

### **Integer solution:**

 $x = -51\,086\,681\,842\,193\,045\,893\,000\,894\,180\,192\,294\,010\,880$ 

### Thence $r_0 = -5.1086681842193045893e+40$

From

$$\Pi(r) = \frac{3\beta^2 r_0^2}{r^4} - \frac{2r_0(1+\beta^2)}{r^3}.$$

 $(3*0.5^{2}(-5.1086681842193045893e+40)^{2})/(1.94973e+13)^{4} - (2*(-5.1086681842193045893e+40)(1+0.5^{2}))/(1.94973e+13)^{3}$ 

### **Input interpretation:**

 $\frac{\frac{3 \times 0.5^2 \left(-5.1086681842193045893 \times 10^{40}\right)^2}{(1.94973 \times 10^{13})^4}}{2 \left(-5.1086681842193045893 \times 10^{40}\right) \left(1+0.5^2\right)} \\ \frac{2 \left(-5.1086681842193045893 \times 10^{40}\right) \left(1+0.5^2\right)}{(1.94973 \times 10^{13})^3}$ 

### **Result:**

 $1.3544992158427489951588703133184468686811765408909185...\times 10^{28}$ 

1.35449921584274899...\*10<sup>28</sup>

Multiplying the two results, we obtain:

 $5.12891528570622599 \times 10^{-14} * (((((3*0.5^{2*}(-5.1086681842193045893e+40)^{2})/(1.94973e+13)^{4} - (2*(-5.1086681842193045893e+40)(1+0.5^{2}))/(1.94973e+13)))))$ 

### Input interpretation:

$$\begin{array}{l} 5.12891528570622599 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left(-5.1086681842193045893 \times 10^{40}\right)^2}{\left(1.94973 \times 10^{13}\right)^4} - \frac{2 \left(-5.1086681842193045893 \times 10^{40}\right) \left(1+0.5^2\right)}{1.94973 \times 10^{13}} \right) \end{array}$$

### **Result:**

 $\begin{array}{l} 1.0306798245571620320462997555761541904197720739669351...\times10^{15}\\ 1.030679824557\ldots\ast10^{15} \end{array}$ 

From which, we obtain:

### Input interpretation:

$$\left( 5.12891528570622599 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193045893 \times 10^{40} \right)^2}{(1.94973 \times 10^{13})^4} - \frac{2 \left( -5.1086681842193045893 \times 10^{40} \right) (1 + 0.5^2)}{1.94973 \times 10^{13}} \right) \right) \uparrow (1/7)$$

### **Result:**

139.551... 139.551... result practically equal to the rest mass of Pion meson 139.57 MeV

### We have that:

 $(((integrate[log base 139.551((((5.1289152857 \times 10^{-14} * (((((3*0.5^{2}(-5.1086681842193e+40)^{2})/(1.94973e+13)^{4} - (2*(-5.1086681842193e+40)(1+0.5^{2}))/(1.94973e+13)))))))]x,[0,4.277])))$ 

### **Definite integral:**

$$\begin{split} \int_{0}^{4.277} &\log_{139.551} \Biggl( 5.1289152857 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193 \times 10^{40} \right)^2}{\left( 1.94973 \times 10^{13} \right)^4} - \frac{2 \left( -5.1086681842193 \times 10^{40} \right) \left( 1 + 0.5^2 \right)}{1.94973 \times 10^{13}} \Biggr) \Biggr) x \, dx = 64.0245 \end{split}$$

### **Input interpretation:**

$$\left( 5.12891528570622599 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193045893 \times 10^{40} \right)^2}{\left( 1.94973 \times 10^{13} \right)^4} - \frac{2 \left( -5.1086681842193045893 \times 10^{40} \right) \left( 1 + 0.5^2 \right)}{1.94973 \times 10^{13}} \right) \right)^{-11 - \pi}$$

### **Result:**

125.409...

125.409... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

We note that:

 $(((integrate[log base 125.409((((5.1289152857 \times 10^{-14} * (((((3*0.5^{2}(-5.1086681842193e+40)^{2})/(1.94973e+13)^{4} - (2*(-5.1086681842193e+40)(1+0.5^{2}))/(1.94973e+13)))))))]x,[0,4.23])))$ 

### **Definite integral:**

$$\begin{split} \int_{0}^{4.23} \log_{125,409} & \left( 5.1289152857 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193 \times 10^{40} \right)^2}{(1.94973 \times 10^{13})^4} - \frac{2 \left( -5.1086681842193 \times 10^{40} \right) (1 + 0.5^2)}{1.94973 \times 10^{13}} \right) \right) x \, dx = 64.0101 \end{split}$$

### Input interpretation:

$$27 \times \frac{1}{2} \left( \left( 5.12891528570622599 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193 \times 10^{40} \right)^2}{(1.94973 \times 10^{13})^4} - \frac{2 \left( -5.1086681842193 \times 10^{40} \right) (1 + 0.5^2)}{1.94973 \times 10^{13}} \right) \right)^{-1} (1/7) - 11 - \frac{1}{2} \right) + \frac{1}{3} + \frac{$$

### **Result:**

### 1729.02... 1729.02...

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

 $[27*1/2(((((((5.12891528570622599 \times 10^{-14} * (((((3*0.5^{2}(-5.1086681842193e+40)^{2})/(1.94973e+13)^{4} - (2*(-5.1086681842193e+40)(1+0.5^{2}))/(1.94973e+13)))))))^{1/7} - 11 - 1/2)))+1/3]^{1/15} - 0.16^{2}$ 

### Input interpretation:

$$\left( 27 \times \frac{1}{2} \left( \left( 5.12891528570622599 \times 10^{-14} \left( \frac{3 \times 0.5^2 \left( -5.1086681842193 \times 10^{40} \right)^2}{(1.94973 \times 10^{13})^4} - \frac{2 \left( -5.1086681842193 \times 10^{40} \right) (1 + 0.5^2)}{1.94973 \times 10^{13}} \right) \right) \right) \right)$$

$$(1/7) - 11 - \frac{1}{2} \right) + \frac{1}{3} \right) ^ (1/15) - 0.16^2$$

### **Result:**

 $1.618216341741066513904570168505155024216978193393542026793\ldots$ 

1.6182163417... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Now, we have that:

From

$$\Pi(r) = \frac{3\beta^2 r_0^2}{r^4} - \frac{2r_0(1+\beta^2)}{r^3},$$
(18)

We obtain:

$$8\pi(P_r + \rho) = \frac{2\beta^2 r_0^2}{r^4} - \frac{r_0}{r^3} - \frac{\beta^2 r_0}{r^3}.$$
(19)

 $(2*0.5^{2}(-5.1086681842193045893e+40)^{2})/(1.94973e+13)^{4} - (-5.1086681842193045893e+40)/(1.94973e+13)^{3} - ((0.5^{2}(-5.1086681842193045893e+40)))/(1.94973e+13)^{3})$ 

### **Input interpretation:**

 $\frac{2 \times 0.5^2 \left(-5.1086681842193045893 \times 10^{40}\right)^2}{(1.94973 \times 10^{13})^4} - \frac{5.1086681842193045893 \times 10^{40}}{(1.94973 \times 10^{13})^3} - \frac{0.5^2 \left(-5.1086681842193045893 \times 10^{40}\right)}{(1.94973 \times 10^{13})^3}$ 

### **Result:**

 $9.0299947722849933010591354192510545392920669827785545\ldots \times 10^{27}$ 

 $9.0299947722849933... \times 10^{27}$ 

From which:

 $P_i = (9.0299947722849933e+27)/((8(x+y)))$ 

### **Input interpretation:**

 $\pi = \frac{9.0299947722849933 \times 10^{27}}{10^{27}}$ 8(x + y)

**Result:** 

 $1.1287493465356242 \times 10^{27}$ x + y

**Alternate forms:** 

 $y = 3.5929207602578262 \times 10^{26} - 1.000000000000000 x$  $1.1287493465356242 \!\times\! 10^{27}$  $\pi =$ 

1.00000000000000 x + 1.00000000000000 y

### **Real solution:**

 $y \approx 0.31830988618379067 (1.1287493465356242 \times 10^{27} - 3.1415926535897932 x)$ 

### Solution:

y ≈

 $6.939957569099423 \times 10^{-7}$  (51771509039990695298421750000000 - 1440931 X)

### Solution for the variable y:

 $y \approx 0.31830988618379067 (1\,128\,749\,346\,535\,624\,162\,500\,000\,000 -$ 3.1415926535897932 x

## **Implicit derivatives:**

 $\frac{\partial x(y)}{\partial y} = -1$  $\frac{\partial y(x)}{\partial x} = -1$ 

From

 $y \approx 0.31830988618379067 (1.1287493465356242 \times 10^{27} - 3.1415926535897932 x)$ 

We obtain:

```
Pi = (9.0299947722849933e+27)/((8(x+((0.31830988618379067))))))
(1.1287493465356242×10^27 - 3.1415926535897932 x))))))
```

### **Input interpretation:**

 $\pi = (9.0299947722849933 \times 10^{27}) / (8 (x + 0.31830988618379067 (1.1287493465356242 \times 10^{27} + x \times (-3.1415926535897932))))$ 

### **Result:**

True

(9.0299947722849933e+27)/((8(x+((0.31830988618379067 (1.1287493465356242×10^27 - 3.1415926535897932 x))))))

### Input interpretation:

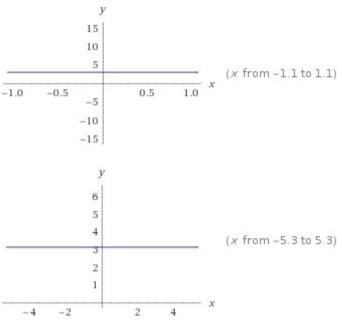
```
\begin{array}{l} \big(9.0299947722849933 \times 10^{27}\big) \big/ \big(8 \, \big(x + 0.31830988618379067 \\ \big(1.1287493465356242 \times 10^{27} + x \times (-3.1415926535897932)\big)\big) \end{array}
```

### **Result:**

 $1.1287493465356242 \times 10^{27}$ 

 $\overline{0.31830988618379067(1.1287493465356242 \times 10^{27} - 3.1415926535897932 x) + x}$ 

### **Plots:**



### Alternate forms:

3.141592653589793

 $\frac{1.128749346535624\times10^{27}}{0.\times10^{-17}\,x+3.592920760257826\times10^{26}}$ 

### **Roots:**

(no roots exist)

### Properties as a real function:

### Domain

### Range

 $\{y \in \mathbb{R} : y \neq 0\}$ 

### Parity

even

R is the set of real numbers

### Series expansion at x = 0:

3.141592653589793

### Series expansion at $x = \infty$ :

3.141592653589793

### Indefinite integral:

 $\int ((9.0299947722849933 \times 10^{27}) / (8 (x + 0.31830988618379067 (1.1287493465356242 \times 10^{27} - 3.1415926535897932 x))))$ 

dx = 3.141592653589793 x + constant

### Limit:

```
\lim_{x \to \pm \infty} \frac{1.1287493465356242 \times 10^{27}}{(0.31830988618379067)} + (0.31830988618379067)
```

From:

 $\frac{1.128749346535624 \times 10^{27}}{0.\times 10^{-17} \, x + 3.592920760257826 \times 10^{26}}$ 

### We obtain:

### **Input interpretation:**

 $1.128749346535624 \times 10^{27}$ 

 $3.592920760257826 \times 10^{26} + 0 \times 10^{-16} x$ 

### **Result:**

3.141592653589792982936689657019144795302800380714842202376...

 $3.1415926535\ldots\approx\pi$ 

### 1/6(((((9.0299947722849933e+27)/((8(x+((0.31830988618379067 (1.1287493465356242×10^27 - 3.1415926535897932 x)))))))))^2 - (5Pi/584)

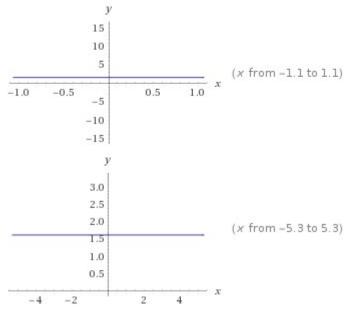
### Input interpretation:

$$\frac{1}{6} \left( \frac{9.0299947722849933 \times 10^{27}}{(8 (x + 0.31830988618379067 (1.1287493465356242 \times 10^{27} + x \times (-3.1415926535897932))))^2 - 5 \times \frac{\pi}{584}} \right)$$

### **Result:**

```
\frac{2.1234584788409976 \times 10^{53} / (0.31830988618379067)}{(1.1287493465356242 \times 10^{27} - 3.1415926535897932 x) + x)^2 - \frac{5 \pi}{584}}
```

### **Plots:**



### Alternate forms:

1.618036869471601

1.618036869471601 result that is a very good approximation to the value of the golden ratio 1,618033988749...

 $2.088736672674086 \!\times\! 10^{53}$ 

 $\overline{(0.\times10^{-17} x + 3.592920760257826\times10^{26})^2}$ 

### Alternate form assuming x is real: 2.1234584788409976×10<sup>53</sup>

 $\frac{2.1234584788409976 \times 10^{53}}{\left(0.\times 10^{-17} \, x + 3.592920760257826 \times 10^{26}\right)^2} - \frac{5 \, \pi}{584}$ 

### **Roots:**

(no roots exist)

### Properties as a real function:

### Domain

### Range

$$\{y \in \mathbb{R} : y > -\frac{5\pi}{584}\}$$

### Parity

even

### Series expansion at x = 0:

1.618036869471601

### Series expansion at $x = \infty$ :

1.618036869471601 1.618036869471601

### Indefinite integral:

 $\int \left(\frac{1}{6} \left( (9.0299947722849933 \times 10^{27}) \right) \right)$ 

 $\begin{array}{l} \left(8\left(x+0.31830988618379067\left(1.1287493465356242\times10^{27}-3.1415926535897932\,x\right)\right)\right)^2 - \end{array}$ 

 $\left(\frac{5\pi}{584}\right)dx = 1.618036869471601 x + \text{constant}$ 

### Limit:

 $\lim_{x \to \pm\infty} \left( -\frac{5\pi}{584} + 2.1234584788409976 \times 10^{53} / (0.31830988618379067 (1.1287493465356242 \times 10^{27} - 3.1415926535897932 x) + x)^2 \right) = 1.618036869471601$ 

ℝ is the set of real numbers

We have also:

 $(((((2*0.5^2*(-5.108668184219e+40)^2)/(1.94973e+13)^4 - (-5.108668184219e+40)/(1.94973e+13)^3 - ((0.5^2*(-5.108668184219e+40)))/(1.94973e+13)^3)))^{1/128}$ 

### **Input interpretation:**

 $\left( \frac{2 \times 0.5^2 \left(-5.108668184219 \times 10^{40}\right)^2}{\left(1.94973 \times 10^{13}\right)^4} - \frac{5.108668184219 \times 10^{40}}{\left(1.94973 \times 10^{13}\right)^3} - \frac{0.5^2 \left(-5.108668184219 \times 10^{40}\right)}{\left(1.94973 \times 10^{13}\right)^3} \right)^{(1/128)}$ 

### **Result:**

1.653498512613571171428644652386508560175050443486348465701...

1.653498512613.... result very near to the 14th root of the following Ramanujan's class invariant  $Q = (G_{505}/G_{101/5})^3 = 1164,2696$  i.e. 1,65578...

From which:

log base 1.65349851261357((((((2\*0.5^2\*(-5.108668184219e+40)^2)/(1.94973e+13)^4 - (-5.108668184219e+40)/(1.94973e+13)^3 - ((0.5^2\*(-5.108668184219e+40)))/(1.94973e+13)^3))))-Pi+1/golden ratio

### **Input interpretation:**

 $\frac{\log_{1.65349851261357} \left( \frac{2 \times 0.5^2 \left(-5.108668184219 \times 10^{40}\right)^2}{\left(1.94973 \times 10^{13}\right)^4} - \frac{5.108668184219 \times 10^{40}}{\left(1.94973 \times 10^{13}\right)^3} - \frac{0.5^2 \left(-5.108668184219 \times 10^{40}\right)}{\left(1.94973 \times 10^{13}\right)^3} \right) - \pi + \frac{1}{\phi}$ 

 $\log_b(x)$  is the base- b logarithm  $\phi$  is the golden ratio

### **Result:**

125.476...

125.476... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV log base 1.65349851261357(((((2\*0.5^2\*(-5.108668184219e+40)^2)/(1.94973e+13)^4 - (-5.108668184219e+40)/(1.94973e+13)^3 - ((0.5^2\*(-5.108668184219e+40)))/(1.94973e+13)^3)))+11+1/golden ratio

### **Input interpretation:**

 $\frac{\log_{1.65349851261357} \left( \frac{2 \times 0.5^2 \left(-5.108668184219 \times 10^{40}\right)^2}{(1.94973 \times 10^{13})^4} - \frac{5.108668184219 \times 10^{40}}{(1.94973 \times 10^{13})^3} - \frac{0.5^2 \left(-5.108668184219 \times 10^{40}\right)}{(1.94973 \times 10^{13})^3} \right) + 11 + \frac{1}{\phi}$ 

 $\log_b(x)$  is the base- b logarithm  $\phi$  is the golden ratio

### **Result:**

139.6180...

139.6180... result practically equal to the rest mass of Pion meson 139.57 MeV

We note that:

(((integrate [log base 1.65349851261357(((((2\*0.5^2\*(-5.1086681e+40)^2)/(1.94973e+13)^4 - (-5.1086681e+40)/(1.94973e+13)^3 -((0.5^2\*(-5.1086681e+40)))/(1.94973e+13)^3)))]x,[0,1])))

### **Definite integral:**

$$\begin{split} \int_{0}^{1} \log_{1.65349851261357} & \left( \frac{2 \times 0.5^{2} \left( -5.1086681 \times 10^{40} \right)^{2}}{\left( 1.94973 \times 10^{13} \right)^{4}} - \right. \\ & \left. - \frac{5.1086681 \times 10^{40}}{\left( 1.94973 \times 10^{13} \right)^{3}} - \frac{0.5^{2} \left( -5.1086681 \times 10^{40} \right)}{\left( 1.94973 \times 10^{13} \right)^{3}} \right) x \, dx = 64. \end{split}$$

Result = 64

 $\log_b(x)$  is the base- b logarithm

# Visual representation of the integral:

### **Indefinite integral:**

$$\int \log_{1.65349851261357} \left( \frac{2 \times 0.5^2 (-5.1086681 \times 10^{40})^2}{(1.94973 \times 10^{13})^4} - \frac{5.1086681 \times 10^{40}}{(1.94973 \times 10^{13})^3} - \frac{0.5^2 (-5.1086681 \times 10^{40})}{(1.94973 \times 10^{13})^3} \right) x \, dx = 64. \, x^2 + \text{constant}$$

sqrt(((integrate [log base 1.65349851261357((((((2\*0.5^2\*(-5.1086681e+40)^2)/(1.94973e+13)^4 - (-5.1086681e+40)/(1.94973e+13)^3 -((0.5^2\*(-5.1086681e+40)))/(1.94973e+13)^3))))]x,[0,1]))),

### Input interpretation:

$$\sqrt{ \left( \int_0^1 \log_{1.65349851261357} \left( \frac{2 \times 0.5^2 \left( -5.1086681 \times 10^{40} \right)^2}{\left( 1.94973 \times 10^{13} \right)^4} - \frac{5.1086681 \times 10^{40}}{\left( 1.94973 \times 10^{13} \right)^3} - \frac{0.5^2 \left( -5.1086681 \times 10^{40} \right)}{\left( 1.94973 \times 10^{13} \right)^3} \right) x \, dx \right)$$

 $\log_b(x)$  is the base– b logarithm

### **Result:**

8.

### **Computation result:**

$$\sqrt{\left(\int_{0}^{1} \log_{1.65349851261357} \left(\frac{2 \times 0.5^{2} (-5.1086681 \times 10^{40})^{2}}{(1.94973 \times 10^{13})^{4}} - \frac{5.1086681 \times 10^{40}}{(1.94973 \times 10^{13})^{3}} - \frac{0.5^{2} (-5.1086681 \times 10^{40})}{(1.94973 \times 10^{13})^{3}}\right) x \, dx \right) = 8.$$

Result = 8

Now, we have (eq.33):

$$8\pi(P_r+\rho) = \frac{\beta^2 r_0^2}{r^4} - \frac{2\gamma^2}{r^2(r^2+\gamma^2)} - \frac{r_0+\beta^2 r_0-\beta^2 r_0^2/r}{r^3} \left(1 - \frac{2\gamma^2}{r^2+\gamma^2}\right).$$

For  $r_0 = 2$  and  $\gamma = 2$   $\beta^2 = 0.5^2$  and r = 1.94973e+13

We obtain:

 $\begin{array}{l} (0.5^{2} * 2^{2})/(1.94973e+13)^{4} - (2^{4})/(((1.94973e+13)^{2}(((1.94973e+13)^{2}+4)))) - (((2+0.5^{2}*2-(0.5^{2}*2^{2})/(1.94973e+13))))/(1.94973e+13)^{3} * ((1-(2^{2}2^{2})/((1.94973e+13)^{2}+2^{2})))) - ((2^{2}2^{2})/((1.94973e+13)^{2}+2^{2}))) + (2^{2}2^{2})/((1.94973e+13)^{2}+2^{2}))) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94973e+13)^{2}+2^{2}))) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94973e+13)^{2})) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94973e+13)^{2}) + (2^{2}2^{2})/((1.94972e+13)^{2}) + (2^{2}2^{2})/((1.9492e+13)^{2}) + (2^{2}2^{2})/((1.9492e+13)^{2}) + (2^{2}2^{$ 

### **Input interpretation:**

 $\frac{ \begin{array}{c} 0.5^2 \times 2^2 \\ \hline (1.94973 \times 10^{13})^4 \end{array} - \frac{ 2 \times 4 }{ (1.94973 \times 10^{13})^2 \left( (1.94973 \times 10^{13})^2 + 4 \right) } - \\ \frac{ 2 + 0.5^2 \times 2 - \frac{ 0.5^2 \times 2^2 }{ 1.94973 \times 10^{13} } }{ (1.94973 \times 10^{13})^3 } \left( 1 - \frac{ 2 \times 2^2 }{ (1.94973 \times 10^{13})^2 + 2^2 } \right)$ 

### **Result:**

 $-3.373001903847483479712390594191421662259557028991392...\times10^{-40} \\ -3.373001903847...*10^{-40}$ 

Now, we have that (eq.32):

$$\Pi(r) = \left(1 - \frac{r_0(1+\beta^2)}{r} + \frac{\beta^2 r_0^2}{r^2}\right) \left[\frac{\gamma^2(2r-3)}{r^2(r^2+\gamma^2)} + \frac{1}{r^2} - \frac{3\gamma^2 r^2 + 2\gamma^4}{r^2(r^2+\gamma^2)^2}\right] - \frac{1}{r^2} - \frac{r_0 r(1+\beta^2) - 2\beta^2 r_0^2}{r^2} \left(\frac{1}{r^2+\gamma^2}\right),$$

For  $r_0 = 2$  and  $\gamma = 2$   $\beta^2 = 0.5^2$  and r = 1.94973e+13

We obtain:

 $((1-(((2(1+0.5^{2})))/(((1.94973e+13))))+(0.5^{2}*2^{2})/(1.94973e+13)^{2}))$ 

**Input interpretation:** 

 $1 - \frac{2\left(1+0.5^2\right)}{1.94973 \times 10^{13}} + \frac{0.5^2 \times 2^2}{\left(1.94973 \times 10^{13}\right)^2}$ 

### **Result:**

0.9999999999999987177711785734698082056782540453820032455146... 0.9999999999999987177711785734698082056782540453820032455146

 $\begin{bmatrix} 4(((2*1.94973e+13-3)))/(((1.94973e+13)^2+4))) + 1/(1.94973e+13)^2 - ((3*4*(1.94973e+13)^2+2*2^4))/(((1.94973e+13)^2*(((1.94973e+13)^2+4))^2))) \end{bmatrix}$ 

### **Input interpretation:**

 $\begin{array}{l} 4 \times \frac{2 \times 1.94973 \times 10^{13} - 3}{(1.94973 \times 10^{13})^2 \left( (1.94973 \times 10^{13})^2 + 4 \right)} \\ \frac{1}{(1.94973 \times 10^{13})^2} - \frac{3 \times 4 \left( 1.94973 \times 10^{13} \right)^2 + 2 \times 2^4}{(1.94973 \times 10^{13})^2 \left( (1.94973 \times 10^{13})^2 + 4 \right)^2} \end{array}$ 

### **Result:**

 $2.6305772007961771383863173578616639074668787230891122...\times10^{-27}$  $2.63057720079\ldots*10^{-27}$ 

 $\begin{array}{l} 0.99999999999998717771178573469808 \quad [4(((2*1.94973e+13-3)))/(((1.94973e+13)^2*(((1.94973e+13)^2+4))))+1/(1.94973e+13)^2-(((3*4*(1.94973e+13)^2+2*2^4))/(((1.94973e+13)^2*(((1.94973e+13)^2+4))^2))] \end{array}$ 

### **Input interpretation:**

### **Result:**

 $2.6305772007958398381959325195544652417132782507985131...\times 10^{-27}$  $2.6305772007958398381959325195544652417132782507985131\times 10^{-27}$  -1/(1.94973e+13)^2 - (((2\*(1.94973e+13)\*(1+0.5^2)-(2\*0.5^2\*2^2))))/(1.94973e+13)^2 \* (1/((1.94973e+13)^2+2^2)))

### Input interpretation:

 $\frac{\overline{(1.94973 \times 10^{13})^2}}{(1.94973 \times 10^{13} \, (1+0.5^2) - 2 \times 0.5^2 \times 2^2}}{(1.94973 \times 10^{13})^2} \times \frac{1}{(1.94973 \times 10^{13})^2 + 2^2}$ 

### **Result:**

 $-2.630577200795435077967471155077888790400968897469797...\times10^{-27} -2.63057720079...*10^{-27}$ 

### From

 $2.6305772007958398381959325195544652417132782507985131 \times 10^{-27}$ 

 $\begin{array}{l}(2.6305772007958398381959325\times10^{-}27)+((-1/(1.94973e+13)^{2}-(((2*(1.94973e+13)*(1+0.5^{2})-(2*0.5^{2}*2^{2}))))/(1.94973e+13)^{2}*\\(1/((1.94973e+13)^{2}+2^{2}))))\end{array}$ 

### **Input interpretation:**

 $\frac{2.6305772007958398381959325 \times 10^{-27} + \left(-\frac{1}{\left(1.94973 \times 10^{13}\right)^2} - \frac{2 \times 1.94973 \times 10^{13} \left(1 + 0.5^2\right) - 2 \times 0.5^2 \times 2^2}{\left(1.94973 \times 10^{13}\right)^2} \times \frac{1}{\left(1.94973 \times 10^{13}\right)^2 + 2^2}\right)$ 

### **Result:**

 $\begin{array}{l} 4.0476022846134492211120959903110253020244150198458536...\times10^{-40} \\ 4.0476022846134492211120959903110253020244150198458536\times10^{-40} \end{array}$ 

From the algebraic sum of the two results (eqs.32 and 33)

(4.047602284613 /10^40 - 3.373001903847/10^40)

### **Input interpretation:**

4.047602284613 3.373001903847 1040

1040

### **Result:**

 $6.74600380766 \times 10^{-41}$ 6.74600380766\*10<sup>-41</sup>

From which, we obtain:

1+(4.047602284613 /10^40 - 3.373001903847/10^40)^1/192

### **Input interpretation:**

 $1 + \overset{192}{1} \sqrt{\frac{4.047602284613}{10^{40}} - \frac{3.373001903847}{10^{40}}}$ 

### **Result:**

1.61769812674436...

1.6176981267443622380497749220352334896454120556052044

From the following possible closed form

 $\frac{1}{12}\sqrt{\frac{1}{13}}(3834 - 605\ e + 1204\ \pi - 1548\ \log(2))} \approx 1.6176981267443622379458$ 

we obtain:

 $1/12 \operatorname{sqrt}(1/13 (3834 - 605 e + 1204 \pi - 1548 \log(2)))$ 

**Input:** 

 $\frac{1}{12}\sqrt{\frac{1}{13}(3834 - 605\ e + 1204\ \pi - 1548\ \log(2))}$ 

log(x) is the natural logarithm

### **Decimal approximation:**

1.617698126744362237945875938599591348477181011119774564239...

1.61769812674... result that is a very good approximation to the value of the golden ratio 1,618033988749...

### Alternate form:

 $\frac{1}{12} \sqrt{\frac{1}{13} \left( 2 \left( 602 \, \pi - 9 \left( 86 \, \log(2) - 213 \right) \right) - 605 \, e \right)}$ 

# Alternative representations:

$$\frac{1}{12}\sqrt{\frac{1}{13}}\left(3834 - 605\ e + 1204\ \pi - 1548\ \log(2)\right)} = \frac{1}{12}\sqrt{\frac{1}{13}}\left(3834 - 605\ e + 1204\ \pi - 1548\ \log_e(2)\right)}$$

$$\frac{1}{12}\sqrt{\frac{1}{13}} (3834 - 605 e + 1204 \pi - 1548 \log(2))} = \frac{1}{12}\sqrt{\frac{1}{13}} (3834 - 605 e + 1204 \pi - 1548 \log(a) \log_a(2))}$$

$$\frac{1}{12}\sqrt{\frac{1}{13}(3834 - 605\ e + 1204\ \pi - 1548\ \log(2))} = \frac{1}{12}\sqrt{\frac{1}{13}(3834 - 605\ e + 1204\ \pi - 3096\ \coth^{-1}(3))}$$

# Series representations:

$$\frac{1}{12} \sqrt{\frac{1}{13} (3834 - 605 e + 1204 \pi - 1548 \log(2))} = \frac{\sqrt{3834 - 605 e + 1204 \pi - 1548 \left(2 i \pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k}\right)}{12 \sqrt{13}} \text{ for } x < 0$$

$$\frac{1}{12} \sqrt{\frac{1}{13}} (3834 - 605 \ e + 1204 \ \pi - 1548 \ \log(2)) = \frac{1}{12 \sqrt{13}} \left( \sqrt{\left( 3834 - 605 \ e + 1204 \ \pi - 1548 \right)} \right) \left( \log(z_0) + \left\lfloor \frac{\arg(2 - z_0)}{2 \ \pi} \right\rfloor \left( \log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \ (2 - z_0)^k \ z_0^{-k}}{k} \right) \right) \right)$$

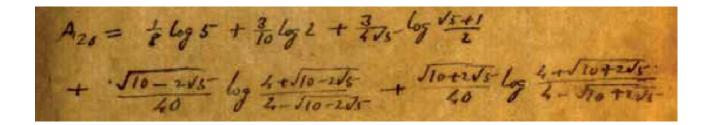
$$\frac{1}{12} \sqrt{\frac{1}{13}} (3834 - 605 \ e + 1204 \ \pi - 1548 \ \log(2))} = \frac{1}{12 \sqrt{13}} \left( \sqrt{\left( 3834 - 605 \ e + 1204 \ \pi - 1548 \right)} \right) \left( 2 \ i \ \pi \left[ \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \ \pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \ (2 - z_0)^k \ z_0^{-k}}{k} \right) \right) \right)$$

#### **Integral representations:**

$$\frac{\frac{1}{12}\sqrt{\frac{1}{13}\left(3834 - 605\ e + 1204\ \pi - 1548\ \log(2)\right)}}{\sqrt{\frac{3834 - 605\ e + 1204\ \pi - 1548\ \int_{1}^{2}\frac{1}{t}\ dt}{12\sqrt{13}}}$$

$$\frac{\frac{1}{12}}{\sqrt{\frac{1}{13}}} \sqrt{\frac{1}{13}} \frac{(3834 - 605\ e + 1204\ \pi - 1548\ \log(2))}{\sqrt{\frac{3834 - 605\ e + 1204\ \pi + \frac{774\ i}{\pi}}{\int_{-i\ \infty + \gamma}^{i\ \infty + \gamma} \frac{\Gamma(-s)^2\ \Gamma(1+s)}{\Gamma(1-s)}} ds}}{\Gamma(1-s)} \quad \text{for } -1 < \gamma < 0$$

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 $\frac{1}{8 \ln 5 + 3}{10 \ln 2 + 3}{(4 \text{sqrt5}) \ln ((\text{sqrt5}+1)/2) + 1}{40(10 - 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 - 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))) + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((((4 + (10 + 2 \text{sqrt5})^{1}/2)))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((4 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln (((10 + (10 + 2 \text{sqrt5})^{1}/2))))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((10 + (10 + 2 \text{sqrt5})^{1}/2)))} + 1}{40(10 + 2 \text{sqrt5})^{1}/2 \ln ((10 + (10 + 2 \text{sqrt5})^{1}/2)))}$ 

$$\begin{array}{l} \text{Input:} \\
 \frac{1}{8} \log(5) + \frac{3}{10} \log(2) + \frac{3}{4\sqrt{5}} \log\left(\frac{1}{2} \left(\sqrt{5} + 1\right)\right) + \\
 \frac{1}{40} \sqrt{10 - 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 - 2\sqrt{5}}}{4 - \sqrt{10 - 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}\right$$

log(x) is the natural logarithm

#### **Exact result:**

Exact result:  

$$\frac{3 \log(2)}{10} + \frac{\log(5)}{8} + \frac{3 \log(\frac{1}{2}(1+\sqrt{5}))}{4\sqrt{5}} + \frac{1}{40} \sqrt{10 - 2\sqrt{5}} \log\left(\frac{4+\sqrt{10-2\sqrt{5}}}{4-\sqrt{10-2\sqrt{5}}}\right) + \frac{1}{40} \sqrt{10 + 2\sqrt{5}} \log\left(\frac{4+\sqrt{10+2\sqrt{5}}}{4-\sqrt{10+2\sqrt{5}}}\right)$$

## **Decimal approximation:**

1.000301163885106499300594205362842555304287694349877380846...

#### 1.0003011638851...

## Alternate forms:

$$\begin{aligned} \frac{3\log(2)}{10} + \frac{\log(5)}{8} + \frac{3\log(\frac{1}{2}(1+\sqrt{5}))}{4\sqrt{5}} + \\ \frac{1}{20}\sqrt{\frac{1}{2}(5-\sqrt{5})} \log(11-4\sqrt{5}+2\sqrt{2(25-11\sqrt{5})}) + \\ \frac{1}{20}\sqrt{\frac{1}{2}(5+\sqrt{5})} \log(11+4\sqrt{5}+2\sqrt{2(25+11\sqrt{5})}) \end{aligned}$$

$$\begin{aligned} \frac{3\log(2)}{10} + \frac{\log(5)}{8} + \frac{1}{40}\sqrt{10-2\sqrt{5}} \left(\log(4+\sqrt{10-2\sqrt{5}}) - \log(4-\sqrt{10-2\sqrt{5}})\right) + \\ \frac{1}{40}\sqrt{10+2\sqrt{5}} \left(\log(4+\sqrt{10+2\sqrt{5}}) - \log(4-\sqrt{10+2\sqrt{5}})\right) + \frac{3\operatorname{csch}^{-1}(2)}{4\sqrt{5}} \\ \frac{1}{40} \left(12\log(2) + 5\log(5) + 6\sqrt{5}\log(\frac{1}{2}(1+\sqrt{5})) + \\ \sqrt{2(5-\sqrt{5})} \log(\frac{4+\sqrt{10-2\sqrt{5}}}{4-\sqrt{10-2\sqrt{5}}}) + \sqrt{2(5+\sqrt{5})}\log(\frac{4+\sqrt{10+2\sqrt{5}}}{4-\sqrt{10+2\sqrt{5}}}) \right) \end{aligned}$$

 $\operatorname{csch}^{-1}(x)$  is the inverse hyperbolic cosecant function

## Alternative representations:

$$\begin{aligned} \frac{\log(5)}{8} + \frac{1}{10}\log(2) 3 + \frac{\log\left(\frac{1}{2}\left(\sqrt{5} + 1\right)\right)3}{4\sqrt{5}} + \frac{1}{40}\sqrt{10 - 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 - 2\sqrt{5}}}{4 - \sqrt{10 - 2\sqrt{5}}}\right) + \\ \frac{1}{40}\sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) = \frac{1}{8}\log(a)\log_a(5) + \\ \frac{3}{10}\log(a)\log_a(2) + \frac{1}{40}\log(a)\log_a\left(\frac{4 + \sqrt{10 - 2\sqrt{5}}}{4 - \sqrt{10 - 2\sqrt{5}}}\right)\sqrt{10 - 2\sqrt{5}} + \\ \frac{3\log(a)\log_a\left(\frac{1}{2}\left(1 + \sqrt{5}\right)\right)}{4\sqrt{5}} + \frac{1}{40}\log(a)\log_a\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right)\sqrt{10 + 2\sqrt{5}} \end{aligned}$$

$$\begin{aligned} \frac{\log(5)}{8} + \frac{1}{10}\log(2) 3 + \frac{\log\left(\frac{1}{2}\left(\sqrt{5} + 1\right)\right)3}{4\sqrt{5}} + \frac{1}{40}\sqrt{10 - 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 - 2\sqrt{5}}}{4 - \sqrt{10 - 2\sqrt{5}}}\right) + \\ \frac{1}{40}\sqrt{10 + 2\sqrt{5}} \log\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right) = \\ \frac{\log_e(5)}{8} + \frac{3\log_e(2)}{10} + \frac{1}{40}\log_e\left(\frac{4 + \sqrt{10 - 2\sqrt{5}}}{4 - \sqrt{10 - 2\sqrt{5}}}\right)\sqrt{10 - 2\sqrt{5}} + \\ \frac{3\log_e\left(\frac{1}{2}\left(1 + \sqrt{5}\right)\right)}{4\sqrt{5}} + \frac{1}{40}\log_e\left(\frac{4 + \sqrt{10 + 2\sqrt{5}}}{4 - \sqrt{10 + 2\sqrt{5}}}\right)\sqrt{10 + 2\sqrt{5}} \end{aligned}$$

$$\begin{aligned} \frac{\log(5)}{8} + \frac{1}{10}\log(2) 3 + \frac{\log\left(\frac{1}{2}\left(\sqrt{5}+1\right)\right)3}{4\sqrt{5}} + \frac{1}{40}\sqrt{10-2\sqrt{5}}\log\left(\frac{4+\sqrt{10-2\sqrt{5}}}{4-\sqrt{10-2\sqrt{5}}}\right) + \\ \frac{1}{40}\sqrt{10+2\sqrt{5}}\log\left(\frac{4+\sqrt{10+2\sqrt{5}}}{4-\sqrt{10+2\sqrt{5}}}\right) = \\ -\frac{\text{Li}_{1}(-4)}{8} - \frac{3\text{Li}_{1}(-1)}{10} - \frac{1}{40}\text{Li}_{1}\left(1 - \frac{4+\sqrt{10-2\sqrt{5}}}{4-\sqrt{10-2\sqrt{5}}}\right)\sqrt{10-2\sqrt{5}} - \\ \frac{3\text{Li}_{1}\left(1 + \frac{1}{2}\left(-1 - \sqrt{5}\right)\right)}{4\sqrt{5}} - \frac{1}{40}\text{Li}_{1}\left(1 - \frac{4+\sqrt{10+2\sqrt{5}}}{4-\sqrt{10+2\sqrt{5}}}\right)\sqrt{10+2\sqrt{5}} - \end{aligned}$$

-(5 (272 - 65  $\pi$  + 4  $\pi$ <sup>2</sup>))/(389 - 483  $\pi$  + 60  $\pi$ <sup>2</sup>)

 $\frac{\text{Input:}}{-\frac{5(272-65 \pi+4 \pi^2)}{389-483 \pi+60 \pi^2}}$ 

#### **Decimal approximation:**

1.000301163885106498494527488341280468516513428439225797725...

#### 1.0003011638851...

Property:  $-\frac{5(272-65\pi+4\pi^2)}{389-483\pi+60\pi^2}$  is a transcendental number

#### **Alternate forms:**

 $\frac{5 \left(272 - 65 \pi + 4 \pi^2\right)}{-389 + 483 \pi - 60 \pi^2}$  $5(272 + \pi (4 \pi - 65))$  $389 - 483 \pi + 60 \pi^2$  $\frac{492\,\pi - 3691}{3\left(389 - 483\,\pi + 60\,\pi^2\right)} - \frac{1}{3}$ 

#### Alternative representations:

$5(272-65\pi+4\pi^2)$	$5\left(272-65\ cos^{-1}(-1)+4\ cos^{-1}(-1)^2\right)$
$\frac{1}{389 - 483 \pi + 60 \pi^2} =$	$= -\frac{1}{389 - 483\cos^{-1}(-1) + 60\cos^{-1}(-1)^2}$
$5(272-65\pi+4\pi^2)$	$5(272-65\pi+24\zeta(2))$
$\frac{1}{389-483\pi+60\pi^2} =$	$\zeta = \frac{1}{389 - 483 \pi + 360 \zeta(2)}$
$5(272-65\pi+4\pi^2)$	$5(272 - 11700^{\circ} + 4(180^{\circ})^2)$
$\frac{-389 - 483 \pi + 60 \pi^2}{-389 - 483 \pi + 60 \pi^2} =$	$389 - 86940^{\circ} + 60(180^{\circ})^2$

#### Series representations:

$$-\frac{5\left(272-65\,\pi+4\,\pi^2\right)}{389-483\,\pi+60\,\pi^2} = -\frac{5\left(-272+65\,\pi-24\sum_{k=1}^{\infty}\frac{1}{k^2}\right)}{-389+483\,\pi-360\sum_{k=1}^{\infty}\frac{1}{k^2}}$$

$$-\frac{5\left(272-65\,\pi+4\,\pi^2\right)}{389-483\,\pi+60\,\pi^2} = -\frac{5\left(-272+65\,\pi+48\,\sum_{k=1}^{\infty}\,\frac{(-1)^k}{k^2}\right)}{-389+483\,\pi+720\,\sum_{k=1}^{\infty}\,\frac{(-1)^k}{k^2}}$$

$$-\frac{5\left(272-65\,\pi+4\,\pi^2\right)}{389-483\,\pi+60\,\pi^2} = -\frac{5\left(-272+65\,\pi-32\,\sum_{k=0}^{\infty}\,\frac{1}{(1+2\,k)^2}\right)}{-389+483\,\pi-480\,\sum_{k=0}^{\infty}\,\frac{1}{(1+2\,k)^2}}$$

 $1/(((-(5 (272 - 65 \pi + 4 \pi^2))/(389 - 483 \pi + 60 \pi^2))))$ 

# Input:

 $\frac{1}{\frac{5(272-65\pi+4\pi^2)}{389-483\pi+60\pi^2}}$ 

#### **Result:**

 $-\frac{389-483\,\pi+60\,\pi^2}{5\left(272-65\,\pi+4\,\pi^2\right)}$ 

#### **Decimal approximation:**

0.999698926787271948180850746057191678463012693318173215823...

0.999698926787... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0**. **989117352243** =  $\phi$ 

Property:  $-\frac{389 - 483 \pi + 60 \pi^2}{5 (272 - 65 \pi + 4 \pi^2)}$  is a transcendental number Input:

 $\frac{1}{512}\sqrt{\frac{-\frac{1}{5(272-65\,\pi+4\,\pi^2)}}{\frac{5(272-65\,\pi+4\,\pi^2)}{389-483\,\pi+60\,\pi^2}}}$ 

#### **Exact result:**

 ${}^{512}_{512} \sqrt{\frac{5 \left(272 - 65 \,\pi + 4 \,\pi^2\right)}{-389 + 483 \,\pi - 60 \,\pi^2}}$ 

#### **Decimal approximation:**

 $1.000000588122329910183597401947347023420199139991757058607\ldots$ 

1.0000005881223299... result very near to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{2\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \frac{e^{-6\pi\sqrt{5}}}{1 + \frac{e^{-8\pi\sqrt{5}}}{1 + \frac{e^{-8\pi\sqrt{5}}}{1 + \dots}}}} \approx 1.0000007913$$

Property:  $512 \sqrt{\frac{5(272 - 65\pi + 4\pi^2)}{-389 + 483\pi - 60\pi^2}}$  is a transcendental number

1/4log base 1.00000058812232991(((1/(((-(5 (272 - 65  $\pi$  + 4  $\pi$ ^2)))/(389 - 483  $\pi$  + 60  $\pi$ ^2))))))))-Pi+1/golden ratio

1

#### Input interpretation:

$$\frac{1}{4} \log_{1.00000058812232991} \left( \frac{1}{-\frac{1}{\frac{5(272-65\pi+4\pi^2)}{389-483\pi+60\pi^2}}} \right) - \pi + \frac{1}{\phi}$$

 $\log_b(x)$  is the base- b logarithm

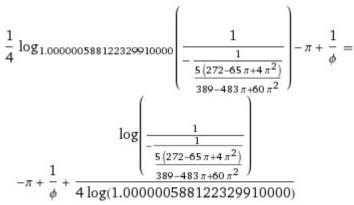
 $\phi$  is the golden ratio

#### **Result:**

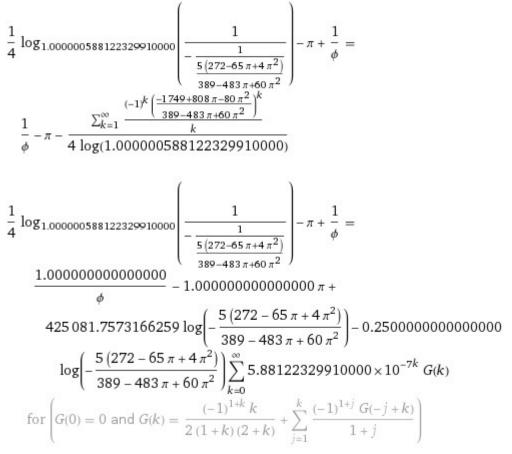
125.476441335...

125.476441335... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Alternative representation:



#### Series representations:



1/4log base 1.00000058812232991(((1/(((-(5 (272 - 65  $\pi$  + 4  $\pi$ ^2)))/(389 - 483  $\pi$  + 60  $\pi$ ^2))))))))+11+1/golden ratio

### Input interpretation:

$$\frac{1}{4} \log_{1.00000058812232991} \left( \frac{1}{-\frac{1}{\frac{5(272-65\pi+4\pi^2)}{389-483\pi+60\pi^2}}} \right) + 11 + \frac{1}{\phi}$$

 $\log_b(x)$  is the base- b logarithm

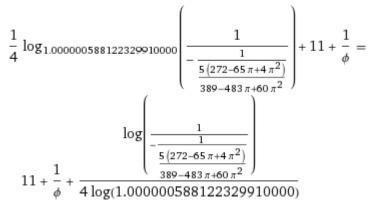
 $\phi$  is the golden ratio

#### **Result:**

139.618033989...

 $139.618033989\ldots$  result practically equal to the rest mass of Pion meson 139.57 MeV

#### Alternative representation:



#### Series representations:

27\*1/8 log base 1.00000058812232991(((1/(((-(5 (272 - 65  $\pi$  + 4  $\pi$ ^2))/(389 - 483  $\pi$  + 60  $\pi$ ^2)))))))))+1

#### Input interpretation:



 $\log_b(x)$  is the base– b logarithm

#### **Result:**

1729.00000000...

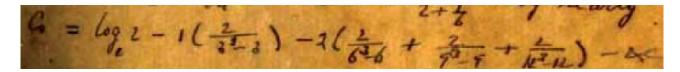
#### 1729

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

## 

#### Series representations:

#### From (page 99):



 $\ln 2 - 1(2/(3^{3}-3))-2(((2/(6^{3}-6)+2/(9^{3}-9)+2/(12^{3}-12))))$ 

#### **Input:**

 $\log(2) - 1 \times \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right)$ 

log(x) is the natural logarithm

#### **Exact result:**

 $\log(2) - \frac{4967}{45045}$ 

#### **Decimal approximation:**

0.582879670292435041906964611190666300565232624092744986610...

#### $0.582879670292435.... = C_0$

#### **Property:**

-  $\frac{4967}{45\,045}$  + log(2) is a transcendental number

#### Alternate form:

45 045 log(2) - 4967 45 045

#### **Alternative representations:**

$$\begin{split} \log(2) &- \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = \\ \log_e(2) &- \frac{2}{24} - 2\left(\frac{2}{-6 + 6^3} + \frac{2}{-9 + 9^3} + \frac{2}{-12 + 12^3}\right) \\ \log(2) &- \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = \\ \log(a) \log_a(2) &- \frac{2}{24} - 2\left(\frac{2}{-6 + 6^3} + \frac{2}{-9 + 9^3} + \frac{2}{-12 + 12^3}\right) \end{split}$$

$$\log(2) - \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = 2 \operatorname{coth}^{-1}(3) - \frac{2}{24} - 2\left(\frac{2}{-6 + 6^3} + \frac{2}{-9 + 9^3} + \frac{2}{-12 + 12^3}\right)$$

## Series representations:

$$\log(2) - \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = -\frac{4967}{45045} + 2i\pi \left\lfloor \frac{\arg(2 - x)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\log(2) - \frac{2}{3^{3} - 3} - 2\left(\frac{2}{6^{3} - 6} + \frac{2}{9^{3} - 9} + \frac{2}{12^{3} - 12}\right) = -\frac{4967}{45045} + \left\lfloor \frac{\arg(2 - z_{0})}{2\pi} \right\rfloor \log\left(\frac{1}{z_{0}}\right) + \log(z_{0}) + \left\lfloor \frac{\arg(2 - z_{0})}{2\pi} \right\rfloor \log(z_{0}) - \sum_{k=1}^{\infty} \frac{(-1)^{k} (2 - z_{0})^{k} z_{0}^{-k}}{k}$$

$$\log(2) - \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = -\frac{4967}{45\,045} + 2\,i\,\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\,\pi}\right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (2 - z_0)^k z_0^{-k}}{k}$$

## Integral representations:

$$\log(2) - \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) = -\frac{4967}{45045} + \int_1^2 \frac{1}{t} dt$$
$$\log(2) - \frac{2}{3^3 - 3} - 2\left(\frac{2}{6^3 - 6} + \frac{2}{9^3 - 9} + \frac{2}{12^3 - 12}\right) =$$

$$-\frac{4967}{45\,045} - \frac{i}{2\,\pi} \int_{-i\,\infty+\gamma}^{i\,\infty+\gamma} \frac{\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)} \,ds \text{ for } -1 < \gamma < 0$$

#### Page 100

2. \$(-2) = (log #) + 2 Co log 2 3.  $\phi(f) + \phi(f) = \frac{3}{2}(l_{1}3)^{2} + 3C_{1}l_{2}s$ 4. \$(-2)" + \$(-3) = 7(492)" + 6Ca 692 5. \$(+2) + \$(= C (3 log 3+4 log 2) + 3 (log 12)

For  $C_0 = 0.582879670292435...$ 

 $(\ln 2)^2+2*0.582879670292435 \ln 2 + 3/2 (\ln 3)^2 + 3*0.582879670292435 \ln 3 + 7 (\ln 2)^2 + 6*0.582879670292435 \ln 2 + 0.582879670292435(3 \ln 3 + 4 \ln 2) + 3/2 (\ln 12)^2 - (\ln 4)^2$ 

#### **Input interpretation:**

$$\begin{split} \log^2(2) + 2 \times 0.582879670292435 \log(2) + \frac{3}{2} \log^2(3) + \\ & 3 \times 0.582879670292435 \log(3) + 7 \log^2(2) + 6 \times 0.582879670292435 \log(2) + \\ & 0.582879670292435 (3 \log(3) + 4 \log(2)) + \frac{3}{2} \log^2(12) - \log^2(4) \end{split}$$

log(x) is the natural logarithm

#### **Result:**

21.6847864965481...

21.6847864...

#### Alternative representations:

$$\begin{split} \log^2(2) + 2 &\times 0.5828796702924350000 \log(2) + \\ &\frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(3) + \\ &7 \log^2(2) + 6 \times 0.5828796702924350000 \log(2) + \\ &0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) = \\ &4.663037362339480000 \log(a) \log_a(2) + 1.748639010877305000 \log(a) \log_a(3) + \\ &0.5828796702924350000 (4 \log(a) \log_a(2) + 3 \log(a) \log_a(3)) + \\ &8 (\log(a) \log_a(2))^2 + \frac{3}{2} (\log(a) \log_a(3))^2 - (\log(a) \log_a(4))^2 + \frac{3}{2} (\log(a) \log_a(12))^2 \end{split}$$

$$\begin{split} \log^2(2) + 2 &\times 0.5828796702924350000 \log(2) + \\ &\frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(3) + \\ &7 \log^2(2) + 6 \times 0.5828796702924350000 \log(2) + \\ &0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) = \\ &4.663037362339480000 \log_e(2) + 1.748639010877305000 \log_e(3) + \\ &0.5828796702924350000 (4 \log_e(2) + 3 \log_e(3)) + \\ &8 \log^2(2) + \frac{3}{2} \log^2(3) - \log^2(4) + \frac{3}{2} \log^2(12) \\ \\ \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \\ &\frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(2) + \\ &0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) = \\ -1.748639010877305000 \text{ Li}_1(-2) + 0.5828796702924350000 \\ &(-3 \text{ Li}_1(-2) - 4 \text{ Li}_1(-1)) - 4.663037362339480000 \text{ Li}_1(-1) + \\ &\frac{3}{2} (-\text{Li}_1(-11))^2 - (-\text{Li}_1(-3))^2 + \frac{3}{2} (-\text{Li}_1(-2))^2 + 8 (-\text{Li}_1(-1))^2 \\ \end{split}$$

From which:

7\*5\*1/(((ln 2)^2+2\*0.582879670292435 ln 2 + 3/2 (ln 3)^2 + 3\*0.582879670292435 ln 3 + 7 (ln 2)^2 + 6\*0.582879670292435 ln 2 + 0.582879670292435((3 ln 3 + 4 ln 2)) + 3/2 (ln 12)^2 - (ln 4)^2))+4/10^3

#### **Input interpretation:**

$$\begin{array}{l} 7\times5\times1\left/\left(\log^2(2)+2\times0.582879670292435\,\log(2)+\frac{3}{2}\,\log^2(3)+3\times0.582879670292435\,\log(3)+7\,\log^2(2)+6\times0.582879670292435\,\log(2)+6\times0.582879670292435\,\log(3)+4\,\log(2))+\frac{3}{2}\,\log^2(12)-\log^2(4)\right)+\frac{4}{10^3}\right)$$

log(x) is the natural logarithm

#### **Result:**

1.61803479833991...

1.61803479833991... result that is almost equal to the value of the golden ratio 1,618033988749...

## Alternative representations:

$$\begin{split} (7 \times 5) &/ \left[ \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(3)}{2} + 3 \times 0.5828796702924350000 \log(3) + 7 \log^2(2) + \\ & 6 \times 0.5828796702924350000 \log(2) + 0.5828796702924350000 \\ & (3 \log(3) + 4 \log(2)) + \frac{3 \log^2(12)}{2} - \log^2(4) \right) + \frac{4}{10^3} = \\ & \frac{4}{10^3} + 35 / \left( 4.663037362339480000 \log_e(2) + 1.748639010877305000 \log_e(3) + \\ & 0.5828796702924350000 (4 \log_e(2) + 3 \log_e(3)) + \\ & 8 \log^2_e(2) + \frac{3}{2} \log^2_e(3) - \log^2_e(4) + \frac{3}{2} \log^2_e(12) \right) \\ & (7 \times 5) / \left( \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(2)}{2} + 3 \times 0.5828796702924350000 \log(2) + \\ & 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{3 \log^2(12)}{2} - \log^2(4) \right) + \\ & \frac{4}{10^3} = \frac{4}{10^3} + 35 / \left( 4.663037362339480000 \log(a) \log_e(2) + \\ & 1.748639010877305000 \log(a) \log_a(3) + 8 (\log(a) \log_e(2))^2 + \\ & \frac{3}{2} (\log(a) \log_a(3))^2 - (\log(a) \log_a(4))^2 + \frac{3}{2} (\log(a) \log_a(12))^2 \right) \\ & (7 \times 5) / \left( \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(3)}{2} + 3 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(2)}{2} + 3 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(2)}{2} + 3 \times 0.5828796702924350000 \log(2) + \\ & \frac{3 \log^2(12)}{2} - \log^2(4) \right) + \\ & \frac{4}{10^3} = \frac{4}{10^3} + 35 / \left( -1.748639010877305000 \ln(-2) + 0.5828796702924350000 \\ & (-3 \ln(-2) - 4 \ln(-1)) - 4.663037362339480000 \ln(-1) + \\ & \frac{3}{2} (-\ln(-1))^2 - (-\ln(-3))^2 + \frac{3}{2} (-\ln(-1))^2 \right) \end{split}$$

# Series representations:

$$\begin{split} (7\times5) \Big/ \left[ \log^2(2) + 2\times 0.58287967029243550000 \log(2) + \\ & \frac{3\log^2(3)}{2} + 3\times 0.58287967029243550000 \log(2) + 0.58287967029243550000 \\ & (3\log(3) + 4\log(2)) + \frac{3\log^2(12)}{2} - \log^2(4) \right) + \frac{4}{10^3} = \frac{1}{250} + 35 \Big/ \\ & \left( 4.663037362339480000 \left[ 2i\pi \left[ \frac{\arg(2-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} \right]^2 + \\ & 8 \left[ 2i\pi \left[ \frac{\arg(2-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} \right]^2 + \\ & 0.5828796702924350000 \\ & \left( 4 \left[ 2i\pi \left[ \frac{\arg(3-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} \right] \right) + \\ & 3 \left[ 2i\pi \left[ \frac{\arg(3-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} \right] \right) + \\ & 1.748639010877305000 \left[ 2i\pi \left[ \frac{\arg(3-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} \right] \right] + \\ & \frac{3}{2} \left[ 2i\pi \left[ \frac{\arg(3-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} \right]^2 - \\ & \left( 2i\pi \left[ \frac{\arg(4-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} \right]^2 + \\ & \frac{3}{2} \left[ 2i\pi \left[ \frac{\arg(4-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} \right]^2 + \\ & \frac{3}{2} \left[ 2i\pi \left[ \frac{\arg(4-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (12-x)^k x^{-k}}{k} \right]^2 \right] \text{ for } x < 0 \end{split}$$

$$\begin{split} (7 \times 5) &/ \left( \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \frac{3 \log^2(3)}{2} + 3 \times 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \times 0.5828796702924350000 \log(2) + 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{3 \log^2(12)}{2} - \log^2(4) \right) + \frac{4}{10^3} = \frac{1}{250} + 35 / \left[ 4.663037362339480000 \\ &\left[ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (2 - z_0)^k z_0^{-k}}{k} \right] + 8 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (2 - z_0)^k z_0^{-k}}{k} \right] + 3 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (2 - z_0)^k z_0^{-k}}{k} \right] + 3 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right] + 3 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right] \right\} + 1.748639010877305000 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right] \right\} + 1.748639010877305000 \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right] \right\} - \frac{3}{2} \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right]^2 - \left\{ 2 i \pi \left[ \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right]^2 \right\}$$

or:

 $(34+1.0864055)/((\ln 2)^2+2*0.582879670292435 \ln 2 + 3/2 (\ln 3)^2 + 3*0.582879670292435 \ln 3 + 7 (\ln 2)^2 + 6*0.582879670292435 \ln 2 + 0.582879670292435(3 \ln 3 + 4 \ln 2) + 3/2 (\ln 12)^2 - (\ln 4)^2)$ 

Where 1.0864055 is the value of the following Ramanujan mock theta function:

 $\frac{0.5^{(2+1)\times(2+2)/2}\,\left(1+0.5\right)\left(1+0.5^2\right)\left(1+0.5^2\right)}{\left(1-0.5\right)\left(1-0.5^3\right)\left(1-0.5^{2\times 2+1}\right)}$ 

 $0.086405529953917050691244239631336405529953917050691244239\ldots \\ 0.0864055\ldots$ 

#### From which, adding 1, we obtain:

 $1 + \frac{0.5^{(2+1)\times(2+2)/2} \left(1+0.5\right) \left(1+0.5^2\right) \left(1+0.5^2\right)}{\left(1-0.5\right) \left(1-0.5^3\right) \left(1-0.5^{2\times 2+1}\right)}$ 

1.086405529953917050691244239631336405529953917050691244239... 1.0864055...

#### Input interpretation:

 $\begin{array}{l} (34+1.0864055) \left/ \left( \log^2(2) + 2 \times 0.582879670292435 \, \log(2) + \frac{3}{2} \, \log^2(3) + \\ 3 \times 0.582879670292435 \, \log(3) + 7 \log^2(2) + 6 \times 0.582879670292435 \, \log(2) + \\ 0.582879670292435 \, (3 \log(3) + 4 \log(2)) + \frac{3}{2} \, \log^2(12) - \log^2(4) \right) \end{array}$ 

log(x) is the natural logarithm

#### **Result:**

1.618019412...

1.618019412... result that is a very good approximation to the value of the golden ratio 1,618033988749...

## Alternative representations:

$$\begin{split} (34 + 1.08641) & \left( \log^2(2) + 2 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \le 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \le 0.5828796702924350000 \log(2) + 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = 35.0864 / \left( 4.663037362339480000 \log_e(2) + 1.748639010877305000 \log_e(3) + 0.5828796702924350000 (4 \log_e(2) + 3 \log_e(3)) + 8 \log^2_e(2) + \frac{3}{2} \log^2_e(3) - \log^2_e(4) + \frac{3}{2} \log^2_e(12) \right) \\ (34 + 1.08641) / \left( \log^2(2) + 2 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = 35.0864 / \left( 4.663037362339480000 \log(a) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = 35.0864 / \left( 4.663037362339480000 \log(a) \log_a(2) + 1.748639010877305000 \log(a) \log_a(3) + 0.5828796702924350000 (4 \log(a) \log_a(2) + 1.748639010877305000 \log(a) \log_a(3) + 0.5828796702924350000 (4 \log(a) \log_a(2) + 3 \log(a) \log_a(3)) + 8 (\log(a) \log_a(2))^2 + \frac{3}{2} (\log(a) \log_a(3))^2 - (\log(a) \log_a(4))^2 + \frac{3}{2} (\log(a) \log_a(12))^2 \right) \\ (34 + 1.08641) / \left( \log^2(2) + 2 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \le 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \le 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = 35.0864 / \left( -1.748639010877305000 Li_1(-2) + 0.5828796702924350000 \log(2) + 0.5828796702924350$$

## Series representations:

$$\begin{split} (34+1.08641) & \left( \log^2(2) + 2 \ge 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \ge 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \ge 0.5828796702924350000 \log(2) + 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = \\ 1.09645 & \left( 0.43716 i \pi \left[ \frac{\arg(2-x)}{2\pi} \right] + i^2 \pi^2 \left[ \frac{\arg(2-x)}{2\pi} \right]^2 + 0.21858 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \right] + 0.1875 i^2 \pi^2 \left[ \frac{\arg(3-x)}{2\pi} \right]^2 - 0.125 i^2 \pi^2 \left[ \frac{\arg(4-x)}{2\pi} \right]^2 + 0.1875 i^2 \pi^2 \left[ \frac{\arg(3-x)}{2\pi} \right] \log(x) - 0.125 i \pi \left[ \frac{\arg(4-x)}{2\pi} \right] \log(x) + 0.1875 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \log(x) - 0.125 i \pi \left[ \frac{\arg(4-x)}{2\pi} \right] \log(x) + 0.1875 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \log(x) - 0.125 i \pi \left[ \frac{\arg(4-x)}{2\pi} \right] \log(x) + 0.1875 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \log(x) - 0.125 i \pi \left[ \frac{\arg(4-x)}{2\pi} \right] \log(x) + 0.1875 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \log(x) + 0.3125 \log^2(x) - 0.21858 \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} - i \left( \pi \left[ \frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} \right) - 0.5 \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} - 0.1875 i \pi \left[ \frac{\arg(3-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} - 0.09375 \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k} \right)^2 - 0.1875 i \pi \left[ \frac{\arg(4-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} + 0.0625 \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} \right)^2 - 0.1875 i \pi \left[ \frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} + 0.0125 i \pi \left[ \frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} + 0.0046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} \right)^2 - 0.1875 i \pi \left[ \frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (4-x)^k x^{-k}}{k} \right)^2 - 0.1875 i \pi \left[ \frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (12-x)^k x^{-k}}{k} - 0.09375 \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k (12-x)^k x^{-k}}{k} + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (12-x)^k x^{-k}}{k} \right)^2 \right)$$

 $(34+1.08641) \left/ \left( log^2(2) + 2 \times 0.5828796702924350000 \ log(2) + 1.08641 \right) \right/ \left( log^2(2) + 2 \times 0.5828796702924350000 \ log(2) + 1.08641 \right) \right/ \left( log^2(2) + 2 \times 0.5828796702924350000 \ log(2) + 1.08641 \right) \right)$  $\frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \times 0.5828796702924350000 \log(2) + 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) = \frac{1}{2} \log^2(12) 3 - \log^2($  $1.09645 \left/ \left[ 0.43716 \, i \, \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \, \pi} \right| + i^2 \, \pi^2 \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \, \pi} \right|^2 + \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \, \pi} \right|^2 \right|^2 \right|^2$  $0.21858 i \pi \left| \frac{\pi - \arg(\frac{3}{z_0}) - \arg(z_0)}{2 \pi} \right| + 0.1875 i^2 \pi^2 \left| \frac{\pi - \arg(\frac{3}{z_0}) - \arg(z_0)}{2 \pi} \right|^2 0.125 i^{2} \pi^{2} \left| \frac{\pi - \arg\left(\frac{4}{z_{0}}\right) - \arg(z_{0})}{2 \pi} \right|^{2} + 0.1875 i^{2} \pi^{2} \left| \frac{\pi - \arg\left(\frac{12}{z_{0}}\right) - \arg(z_{0})}{2 \pi} \right|^{2} + 0.1875 i^{2} \pi^{2} \left| \frac{\pi - \arg\left(\frac{12}{z_{0}}\right) - \arg(z_{0})}{2 \pi} \right|^{2} + 0.1875 i^{2} \pi^{2} \left| \frac{\pi - \arg\left(\frac{12}{z_{0}}\right) - \arg(z_{0})}{2 \pi} \right|^{2} \right|^{2}$  $0.32787 \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg(z_0)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right) - \arg\left(\frac{\pi - \arg\left(\frac{2}{z_0}\right)}{2 \pi}\right)}{2 \pi \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{2}{z_0}\right)}{2 \pi} \right| \log(z_0) + i \pi \left| \frac{\pi - \arg\left(\frac{\pi - \arg\left(\frac{\pi$  $0.1875 i\pi \left| \frac{\pi - \arg(\frac{3}{z_0}) - \arg(z_0)}{2\pi} \right| \log(z_0) - \frac{1}{2\pi} \log(z_0) + \frac{1}{2$  $0.125 i\pi \left| \frac{\pi - \arg\left(\frac{4}{z_0}\right) - \arg(z_0)}{2\pi} \right| \log(z_0) + 0.1875 i\pi \left| \frac{\pi - \arg\left(\frac{12}{z_0}\right) - \arg(z_0)}{2\pi} \right|$  $\log(z_0) + 0.3125 \log^2(z_0) - 0.21858 \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^$  $i\left[\pi \left| \frac{\pi - \arg\left(\frac{z}{z_0}\right) - \arg(z_0)}{2\pi} \right| \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right| 0.5 \log(z_0) \sum_{k=0}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} +$  $0.25 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right)^2 - 0.10929 \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k (2-z_0)^k}{k} - \frac{1}{2} \sum_$  $0.1875 i\pi \left| \frac{\pi - \arg\left(\frac{3}{z_0}\right) - \arg(z_0)}{2\pi} \right| \sum_{k=1}^{\infty} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} - \frac{1}{z_0} \frac{(-1)^k (3 - z_0)^k z_0^{-k}}{k} \right|$  $0.09375 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} \right)^2 + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right)^2 + 0.046875 \left( \sum_{k=1}^{\infty} \frac{(-1)$  $0.125 i\pi \left| \frac{\pi - \arg\left(\frac{4}{z_0}\right) - \arg(z_0)}{2\pi} \right| \sum_{i=1}^{\infty} \frac{(-1)^k (4 - z_0)^k z_0^{-k}}{k} + \frac{1}{2\pi} \frac{1}{z_0} \frac{(-1)^k (4 - z_0)^k z_0^{-k}}{k} + \frac{1}{2\pi} \frac{(-1)^k (4 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (4 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (4 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (4 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k (2 - z_0)^k}{k} + \frac{1}{2\pi} \frac{(-1)^k (2 - z_0)^k}{k} + \frac{1}{2\pi$  $0.0625 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} - 0.03125 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} \right)^2 -$  $0.1875 i\pi \left| \frac{\pi - \arg\left(\frac{1z}{z_0}\right) - \arg(z_0)}{2\pi} \right| \sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left| \frac{1}{2\pi} \right|^2 \frac{(-1)^k (12 - z_0)^k (12 - z_0$  $0.09375 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} + 0.046875 \left[ \sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} \right]^2$   $(34 + 1.08641) / (\log^2(2) + 2 \times 0.5828796702924350000 \log(2) +$  $\frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(3) +$  $4.3858 \left/ \left[ 0.87432 \left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) + 0.43716 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) + \right. \right]$  $\left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor^2 \log^2 \left(\frac{1}{z_0}\right) + 0.1875 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor^2 \log^2 \left(\frac{1}{z_0}\right) - 0.125 \left\lfloor \frac{\arg(4-z_0)}{2\pi} \right\rfloor^2 \log^2 \left(\frac{1}{z_0}\right) + 0.1875 \left\lfloor \frac{\arg(12-z_0)}{2\pi} \right\rfloor^2 \log^2 \left\lfloor \frac{1}{z_0} \right\rfloor^2 \log^2 \left\lfloor \frac{1}{$  $1.31148 \log(z_0) + 0.87432 \left[ \frac{\arg(2-z_0)}{2\pi} \right] \log(z_0) + \\ 0.43716 \left[ \frac{\arg(3-z_0)}{2\pi} \right] \log(z_0) + 2 \left[ \frac{\arg(2-z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) \log(z_0) +$  $2\left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor^2 \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor^2 \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left\lfloor \frac{1}{z_0} \right\rfloor^2 \log(z_0) + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\rfloor^2 \log(z_0) + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0} + 0.375 \left\lfloor \frac{1}{z_0} \right\lfloor \frac{1}{z_0}$  $0.375 \left[\frac{\arg(3-z_0)}{2\pi}\right]^2 \log\left(\frac{1}{z_0}\right) \log(z_0) - 0.25 \left[\frac{\arg(4-z_0)}{2\pi}\right] \log\left(\frac{1}{z_0}\right) \log(z_0) - 0.25 \left[\frac{\arg(4-z_0)}{2\pi}\right] \log\left(\frac{1}{z_0}\right) \log(z_0) - 0.25 \left[\frac{\arg(4-z_0)}{2\pi}\right]^2 \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left[\frac{\arg(12-z_0)}{2\pi}\right] \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left[\frac{\arg(12-z_0)}{2\pi}\right] \log\left(\frac{1}{z_0}\right) \log(z_0) + 0.375 \left[\frac{\arg(12-z_0)}{2\pi}\right] \log\left(\frac{1}{z_0}\right) \log(z_0) + 1.25 \log^2(z_0) + 2 \left[\frac{\arg(2-z_0)}{2\pi}\right]$ 
$$\begin{split} &\log^2(z_0) + \left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor^2 \log^2(z_0) + 0.375 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor \log^2(z_0) + \\ &0.1875 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor^2 \log^2(z_0) - 0.25 \left\lfloor \frac{\arg(4-z_0)}{2\pi} \right\rfloor \log^2(z_0) - \\ &0.125 \left\lfloor \frac{\arg(4-z_0)}{2\pi} \right\rfloor^2 \log^2(z_0) + 0.375 \left\lfloor \frac{\arg(12-z_0)}{2\pi} \right\rfloor \log^2(z_0) + \end{split}$$
 $0.1875 \left\lfloor \frac{\arg(12-z_0)}{2\pi} \right\rfloor^2 \log^2(z_0) - 0.87432 \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k (2-z$  $2\left\lfloor \frac{\arg(2-z_0)}{2\pi} \right\rfloor \log \left(\frac{1}{z_0}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k}$  $2\log(z_0)\sum_{k=1}^{\infty}\frac{(-1)^k\left(2-z_0\right)^kz_0^{-k}}{k} - 2\Big\lfloor\frac{\arg(2-z_0)}{2\pi}\Big\rfloor\log(z_0)\sum_{k=1}^{\infty}\frac{(-1)^k\left(2-z_0\right)^kz_0^{-k}}{k} + \frac{2\log(z_0)^k(z_0)^k(2-z_0)^k(z_0)^{-k}}{k}\Big\rfloor$  $\left(\sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k}\right)^2 - 0.43716 \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} - \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} -$  $0.375 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor \log \left(\frac{1}{z_0}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} - \frac{1}{2} \left\lfloor \frac{\log(3-z_0)^k (3-z_0)^k (3-z_0)^k (3-z_0)^k}{k} \right\rfloor$  $0.375 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} - 0.375 \left\lfloor \frac{\arg(3-z_0)}{2\pi} \right\rfloor \log(z_0)$  $\sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} + 0.1875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k} \right)^2 +$  $0.25 \left\lfloor \frac{\arg(4-z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} +$  $0.25 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} + 0.25 \left\lfloor \frac{\arg(4-z_0)}{2\pi} \right\rfloor \log(z_0)$  $\sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} - 0.125 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (4-z_0)^k z_0^{-k}}{k} \right)^2 -$  $0.375 \left\lfloor \frac{\arg(12-z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{2\pi}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{2\pi}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{2\pi}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{2\pi}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k z_0^{-k}}{k} - \frac{1}{2\pi} \left\lfloor \frac{1}{2\pi} \right\rfloor \log\left(\frac{1}{2\pi}\right) \sum_{k=1}^{\infty} \frac{(-1)^k (12-z_0)^k (12-z$  $0.375 \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} - 0.375 \left\lfloor \frac{\arg(12 - z_0)}{2\pi} \right\rfloor \log(z_0)$  $\sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} + 0.1875 \left( \sum_{k=1}^{\infty} \frac{(-1)^k (12 - z_0)^k z_0^{-k}}{k} \right)^2 \right)$ 

#### Integral representation:

$$\begin{split} (34+1.08641) \left/ \left( \log^2(2) + 2 \times 0.5828796702924350000 \log(2) + \frac{1}{2} \log^2(3) 3 + 3 \times 0.5828796702924350000 \log(3) + 7 \log^2(2) + 6 \times 0.5828796702924350000 \log(2) + 0.5828796702924350000 (3 \log(3) + 4 \log(2)) + \frac{1}{2} \log^2(12) 3 - \log^2(4) \right) = \\ (17.5432 i^2 \pi^2) \right/ \left( \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{\Gamma(-s)^2 \ \Gamma(1 + s)}{\Gamma(1 - s)} \ ds \right)^2 + 0.1875 \\ \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1 + s)}{\Gamma(1 - s)} \ ds \right)^2 - 0.125 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{3^{-s} \ \Gamma(-s)^2 \ \Gamma(1 + s)}{\Gamma(1 - s)} \ ds \right)^2 + 0.1875 \\ \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{11^{-s} \ \Gamma(-s)^2 \ \Gamma(1 + s)}{\Gamma(1 - s)} \ ds \right)^2 + 1.74864 \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ (0.5 + 2^s) \ i \ \pi \ \Gamma(-s)^2 \ \Gamma(1 + s)}{\Gamma(1 - s)} \ ds \right) \text{ for } -1 < \gamma < 0 \end{split}$$

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 $C_0 = 0.582879670292435$ ; q = -072815845483680; x = 2, n = 3, we obtain:

2 ln 3 (ln 2/(sqrt(2Pi))) – 2 (ln 3)^2 – (3-1) (((1/2\*0.582879670292435^2-0.072815845483680 – (Pi^2)/24 – 1/2(ln((2Pi)))^2)))

#### Input interpretation:

$$2 \log(3) \times \frac{\log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3-1) \left( \frac{1}{2} \times 0.582879670292435^2 - 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \right)$$

 $\log(x)$  is the natural logarithm

#### **Result:**

2.19983330532390...

2.1998333053239...

## Alternative representations:

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \\ & \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) = \\ & - 2\log_e^2(3) - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\log_e^2(2\pi)\right) + \frac{2\log_e(2)\log_e(3)}{\sqrt{2\pi}} \end{aligned}$$

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) = -2\left(\log(a)\log_a(3)\right)^2 - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\left(\log(a)\log_a(2\pi)\right)^2\right) + \frac{2\log^2(a)\log_a(2)\log_a(3)}{\sqrt{2\pi}}$$

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ \left(\frac{0.5828796702924350000^2}{2} - 0.072815845483680000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) = -2(-\text{Li}_1(-2))^2 - 2\left(-0.072815845483680000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}(-\text{Li}_1(1-2\pi))^2\right) + \frac{2\text{Li}_1(-2)\text{Li}_1(-1)}{\sqrt{2\pi}}$$

#### Series representations: (2 log(3)) log(2)

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \left( \frac{0.5828796702924350000^2}{2} - \\ & 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi) \right) = \\ & -0.194117019072857733 + 0.0833333333333333333337^2 - \\ & 2.0000000000000000 \log^2(3) + \log^2(2\pi) + \\ & \frac{2\log(2)\log(3)}{\exp\left(i\pi \left\lfloor \frac{\arg(2\pi-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2\pi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \end{aligned}$$
 for  $(x \in \mathbb{R} \text{ and } x < 0)$   
$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ & \left( \frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi) \right) = \\ -0.194117019072857733 + \frac{\pi^2}{12} - 2\log^2(3) + \log^2(2\pi) + \\ & \frac{2\log(2)\log(3) \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(2\pi-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(2\pi-z_0)/(2\pi) \rfloor)}}{\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2\pi-z_0)^k z_0^{-k}}{k!}} \end{aligned}$$

## Integral representations:

Subtracting  $C_0 = 0.582879670292435$ ; we obtain:

2 ln 3 (ln 2/(sqrt(2Pi))) – 2 (ln 3)^2 – (3-1) (((1/2\*0.582879670292435^2-0.072815845483680 – (Pi^2)/24 – 1/2(ln((2Pi)))^2)))-0.582879670

#### Input interpretation:

$$2 \log(3) \times \frac{\log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \left( \frac{1}{2} \times 0.582879670292435^2 - 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \right)$$
  
0.582879670

 $\log(x)$  is the natural logarithm

#### **Result:**

1.616953635323902039379912145264828435936089063414023486361...

1.61695363532... result that is near to the value of the golden ratio 1,618033988749...

## Alternative representations:

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \\ & \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ & 0.58288 = -0.58288 - 2\log_e^2(3) - \\ & 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\log_e^2(2\pi)\right) + \\ & \frac{2\log_e(2)\log_e(3)}{\sqrt{2\pi}} \end{aligned}$$

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ 0.58288 = -0.58288 - 2\left(\log(a)\log_a(3)\right)^2 - \\ 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\left(\log(a)\log_a(2\pi)\right)^2\right) + \frac{2\log^2(a)\log_a(2)\log_a(3)}{\sqrt{2\pi}}$$

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \\ & \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ & 0.58288 = -0.58288 - 2\left(-\text{Li}_1(-2)\right)^2 - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\left(-\text{Li}_1(1-2\pi)\right)^2\right) + \frac{2\text{Li}_1(-2)\text{Li}_1(-1)}{\sqrt{2\pi}} \end{aligned}$$

## Series representations:

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - 0.58288 = -0.776997 + 0.0833333 \pi^2 - 2\log^2(3) + \log^2(2\pi) + \frac{2\log(2)\log(3)}{\sqrt{-1+2\pi} \sum_{k=0}^{\infty} (-1+2\pi)^{-k} \left(\frac{1}{2} \atop k\right)}$$

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \\ \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ \frac{0.58288 = -0.776997 + 0.0833333 \pi^2 - 2\log^2(3) + \log^2(2\pi) + \\ \frac{2\log(2)\log(3)}{\exp\left(i\pi\left\lfloor\frac{\arg(2\pi-x)}{2\pi}\right\rfloor\right)\sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2\pi-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}} \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)$$

$$\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - 0.58288 = -0.776997 + \frac{\pi^2}{12} - 2\log^2(3) + \log^2(2\pi) + 2\log(2)\log(3)$$

$$\frac{2\log(2)\log(3)}{\exp\left(i\pi\left\lfloor\frac{\arg(2\pi-x)}{2\pi}\right\rfloor\right)\sqrt{x}\sum_{k=0}^{\infty}\frac{(-1)^k(2\pi-x)^kx^{-k}\left(-\frac{1}{2}\right)_k}{k!} \quad \text{for } (x \in \mathbb{R} \text{ and } x < 0)$$

## Integral representations:

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \\ & \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ & 0.58288 = \frac{1}{\sqrt{2\pi}} 0.0833333 \left(\int_0^1 \int_0^1 \frac{1}{(1+t_1)(1+2t_2)} dt_2 dt_1 - \\ & 9.32396\sqrt{2\pi} + \pi^2 \sqrt{2\pi} - 24 \left(\int_1^3 \frac{1}{t} dt\right)^2 \sqrt{2\pi} + 12 \left(\int_1^{2\pi} \frac{1}{t} dt\right)^2 \sqrt{2\pi} \right) \end{aligned}$$

$$\begin{aligned} \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} &- 2\log^2(3) - (3-1) \\ & \left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) - \\ & 0.58288 = \frac{1}{i^2 \pi^2 \sqrt{2\pi}} 0.0833333 \\ & \left(6\left(\int_{-i \, \infty+\gamma}^{i \, \infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} \, ds\right) \int_{-i \, \infty+\gamma}^{i \, \infty+\gamma} \frac{2^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} \, ds - \\ & 9.32396 \, i^2 \pi^2 \sqrt{2\pi} + i^2 \pi^4 \sqrt{2\pi} - 6\left(\int_{-i \, \infty+\gamma}^{i \, \infty+\gamma} \frac{2^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} \, ds\right)^2 \sqrt{2\pi} + \\ & 3\left(\int_{-i \, \infty+\gamma}^{i \, \infty+\gamma} \frac{(-1+2\pi)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} \, ds\right)^2 \sqrt{2\pi} \right) \text{ for } -1 < \gamma < 0 \end{aligned}$$

We have also:

$$((((2/((2 \ln 3 (\ln 2/(sqrt(2Pi))) - 2 (\ln 3)^2 - (3-1) (((1/2*0.582879670292435^2 - 0.072815845483680 - (Pi^2)/24 - 1/2(\ln((2Pi)))^2))))))^{1/128})$$

#### Input interpretation:

 $\left( 2 \left/ \left( 2 \log(3) \times \frac{\log(2)}{\sqrt{2\pi}} - 2 \log^2(3) - (3-1) \left( \frac{1}{2} \times 0.582879670292435^2 - 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2\pi) \right) \right) \right) (1/128)$ 

log(x) is the natural logarithm

#### **Result:**

0.99925625791158988...

0.99925625791158988... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0**. 989117352243 =  $\phi$ 

 $\begin{array}{l} sqrt[1/2log \ base \ 0.99925625791158988((((2/((2 \ ln \ 3 \ (ln \ 2/(sqrt(2Pi))) - 2 \ (ln \ 3)^2 - (3-1) \ (((1/2*0.582879670292435^2 - 0.072815845483680 - (Pi^2)/24 - 1/2(ln((2Pi)))^2)))))))] \end{array}$ 

#### Input interpretation:

$$\sqrt{ \left( \frac{1}{2} \log_{0.99925625791158988} \right) }$$

$$2 \left/ \left( 2 \log(3) \times \frac{\log(2)}{\sqrt{2\pi}} - 2 \log^2(3) - (3-1) \left( \frac{1}{2} \times 0.582879670292435^2 + 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2\pi) \right) \right)$$

log(x) is the natural logarithm

### **Result:**

8.0000000000000...

 $8.000000000000 e^0 \approx 8.0000$  (real, principal root)

 $8.000000000000 e^{i\pi} \approx -8.0000$  (real root)

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## Alternative representations:

$$\sqrt{\left(\frac{1}{2}\log_{0.000256257911589880000}\right)^{2} - 2\log^{2}(3) - (3 - 1)\left(\frac{0.5828796702924350000^{2}}{2} - 0.0728158454836800000 - \frac{\pi^{2}}{24} - \frac{1}{2}\log^{2}(2\pi)\right)\right)} = \sqrt{\left(\log\left(2/\left(-2\log^{2}(3) - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^{2}}{2} - \frac{\pi^{2}}{24} - \frac{1}{2}\log^{2}(2\pi)\right)\right) + \frac{2\log(2)\log(3)}{\sqrt{2\pi}}\right)} \right) / (2\log(0.999256257911589880000)) \right)$$

$$\begin{split} \sqrt{\left[\frac{1}{2}\log_{0.999256257911589880000}\right]} & 2\left/\left(\frac{2\log(3)\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right)\right)\right) = \\ \sqrt{\left(\frac{1}{2}\log_{0.999256257911589880000}\left[2\left/\left(-2\log_e^2(3) - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\log_e^2(2\pi)\right) + \frac{2\log_e(2)\log_e(3)}{\sqrt{2\pi}}\right)\right)\right)} \end{split}$$

$$\begin{split} \sqrt{\left(\frac{1}{2}\log_{0.999256257911589880000}\right)} & 2\left/\left(\frac{2\log(3)\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right)\right)\right) = \\ \sqrt{\left(\frac{1}{2}\log_{0.999256257911589880000}\left(2\left/\left(-2\left(\log(a)\log_a(3)\right)^2 - 2\left(-0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2}\left(\log(a)\log_a(2\pi)\right)^2\right) + \frac{2\log^2(a)\log_a(2)\log_a(3)}{\sqrt{2\pi}}\right)\right)} \end{split}$$

## Integral representations:

$$\begin{split} &\sqrt{\left(\frac{1}{2}\log_{0.555257911589880000}\right)} \\ & 2\left/\left(\frac{2\log(3)\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right)\right)\right) = \\ & \sqrt{\left(\frac{1}{2}\log_{0.555257911589880000}\left(-\left(\left(1.0000000000000000\sqrt{2\pi}\right)\right)\right) - \left(\int_{0}^{1}\int_{0}^{1}\frac{1}{(1+t_1)(1+2t_2)}dt_2dt_1 + \left(0.097058509536428866 - 0.041666666666666666667\pi^2 + \left(\int_{1}^{3}\frac{1}{t}dt\right)^2 - 0.50000000000000\left(\int_{1}^{2\pi}\frac{1}{t}dt\right)^2\right)\sqrt{2\pi}\right)\right)} \end{split}$$

$$\begin{split} \sqrt{\left(\frac{1}{2}\log_{0.500256257911589880000}\right)} & 2\left/\left(\frac{2\log(3)\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right)\right)\right) = \\ & \sqrt{\left(\frac{1}{2}\log_{0.500256257911589880000}\left(2\left/\left(-\frac{\left(\int_{-i\,\infty+\gamma}^{i\,\omega+\gamma}\frac{2^{-5}\Gamma(-s)^2}{\Gamma(1-s)}ds\right)^2}{2i^2\pi^2} - 2\left(0.097058509536428866 - \frac{\pi^2}{24} - \frac{\left(\int_{-i\,\infty+\gamma}^{i\,\omega+\gamma}\frac{(-1+2\pi)^{-5}\Gamma(-s)^2}{\Gamma(1-s)}ds\right)^2}{8i^2\pi^2}\right) + \\ & \frac{\left(\int_{-i\,\infty+\gamma}^{i\,\omega+\gamma}\frac{\Gamma(-s)^2}{\Gamma(1-s)}ds\right)\int_{-i\,\omega+\gamma}\frac{2^{-5}\Gamma(-s)^2\Gamma(1+s)}{\Gamma(1-s)}ds}{2i^2\pi^2\sqrt{2\pi}}\right)\right)}{2i^2\pi^2\sqrt{2\pi}} \end{split}$$
for  $-1 < \gamma < 0$ 

 $\Gamma(x)$  is the gamma function

 $[ log base 0.99925625791158988((((2/((2 ln 3 (ln 2/(sqrt(2Pi))) - 2 (ln 3)^2 - (3-1)))))) - 2 (ln 3)^2 - (3-1)) (((1/2*0.582879670292435^2 - 0.072815845483680 - (Pi^2)/24 - 1/2(ln((2Pi)))^2)))))) - Pi + 1/golden ratio ) ] ] - Pi + 1/golden ratio ] ] [ Pi + 1/golden ratio ] ] ] - Pi + 1/golden ratio ] ] [ Pi + 1/golden ratio ] ] ] - Pi + 1/golden ratio ] ] [ Pi + 1/golden ratio ] [ Pi + 1/golden ratio ] ]$ 

## Input interpretation:

$$\begin{split} \log_{0.00025625791158988} \Biggl( & 2 \left/ \left( 2 \log(3) \times \frac{\log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \left( \frac{1}{2} \times 0.582879670292435^2 - 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \right) \Biggr) - \pi + \frac{1}{\phi} \end{split}$$

log(x) is the natural logarithm

 $\log_b(x)$  is the base- b logarithm

 $\phi$  is the golden ratio

#### **Result:**

125.47644133516...

125.47644... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

## Alternative representations:

$$\begin{split} \log_{0.000256257011589880000} \bigg| \\ & 2 \Big/ \bigg( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \bigg( \frac{0.5828796702924350000^2}{2} - \\ & 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) \bigg) - \pi + \frac{1}{\phi} = \\ & -\pi + \frac{1}{\phi} + \log \bigg( 2 \Big/ \bigg( -2 \log^2(3) - 2 \bigg( -0.0728158454836800000 + \\ & \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) + \\ & \frac{2 \log(2) \log(3)}{\sqrt{2 \pi}} \bigg) \bigg) \Big/ \log(0.999256257911589880000) \\ \\ & \log_{0.000256257911589880000} \bigg( \\ & 2 \Big/ \bigg( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \bigg( \frac{0.5828796702924350000^2}{2} - \\ & 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) \bigg) \bigg) - \\ & \pi + \frac{1}{\phi} = -\pi + \log_{0.000256257911589880000} \bigg( \\ & 2 \Big/ \bigg( -2 \log^2_e(3) - 2 \bigg( -0.0728158454836800000 + \\ & \frac{0.5828796702924350000^2}{2} - \\ & \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) + \frac{2 \log_e(2) \log_e(3)}{\sqrt{2 \pi}} \bigg) \bigg) + \frac{1}{\phi} \end{split}$$

log<sub>0.999256257911589880000</sub>

$$2 \left/ \left( \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \left( \frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi) \right) \right) - \pi + \frac{1}{\phi} = -\pi + \log_{0.999256257911589880000} \left( 2 \left/ \left( -2 \left( \log(a) \log_a(3) \right)^2 - 2 \left( -0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2} \left( \log(a) \log_a(2\pi) \right)^2 \right) + \frac{2\log^2(a) \log_a(2) \log_a(3)}{\sqrt{2\pi}} \right) \right) + \frac{1}{\phi}$$

## Series representation:

$$\begin{split} \log_{0.999256257911589880000} \Biggl( & 2 \Big/ \bigg( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \bigg( \frac{0.5828796702924350000^2}{2} - \\ & 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) \Biggr) - \pi + \frac{1}{\phi} = \\ & \frac{1}{\phi} - \pi - \Biggl( \sum_{k=1}^{\infty} \frac{1}{k} (-1)^k \bigg( -1 - \bigg( 1.0000000000000 \sqrt{2 \pi} \bigg) \Big/ \\ & \bigg( -1.0000000000000000 \log(2) \log(3) + \\ & (0.097058509536428866 - 0.04166666666666666667 \pi^2 + \\ & \log^2(3) - 0.5000000000000 \log^2(2 \pi) \bigg) \\ & \sqrt{2 \pi} \bigg) \Biggr)^k \Biggr) \Big/ \log(0.999256257911589880000) \end{split}$$

#### **Integral representations:**

log0.999256257911589880000  $2 \Big/ \left( \frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1) \left( \frac{0.5828796702924350000^2}{2} - \right) \right) \Big) \Big) + \frac{1}{\sqrt{2\pi}} - \frac{1}{\sqrt{2\pi}} + \frac{1}{\sqrt{2\pi}} - \frac{1}{\sqrt{2\pi}} + \frac$  $0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi) \bigg) - \pi + \frac{1}{\phi} =$  $-\frac{1}{\phi} \left(-1 + \phi \pi - \phi \log_{0.999256257911589880000} \left(-\left(\left(1.00000000000000000\sqrt{2 \pi}\right)\right)\right)\right)$  $0.0416666666666666666667 \pi^2 + \left(\int_1^3 \frac{1}{t} dt\right)^2 0.500000000000000 \left( \int_{1}^{2\pi} \frac{1}{t} dt \right)^{2} \sqrt{2\pi} \right) \right) \right)$ log<sub>0.999256257911589880000</sub>  $2 \left/ \left( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \, \pi}} - 2 \log^2(3) - (3 - 1) \left( \frac{0.5828796702924350000^2}{2} \right. \right. \right. \right. \\$  $0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2\pi) \bigg| \bigg| \pi + \frac{1}{\phi} = -\frac{1}{\phi} \left| -1 + \phi \,\pi - \phi \log_{0.999256257911589880000} \right|$  $2 \left/ \left( -\frac{\left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2}{2 \ i^2 \ \pi^2} - 2 \left( 0.097058509536428866 - \right)^2 \right)^2 \right) \right|_{-s} = -\frac{1}{2} \left( -\frac{1}{2} \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2}{2 \ i^2 \ \pi^2} \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(1+s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)^2 \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{2^{-s} \ \Gamma(-s)}{\Gamma(1-s)} \ ds \right)^2 - 2 \left( \int_{-i \ \infty + \gamma} \frac$  $\frac{\pi^2}{24} - \frac{\left(\int_{-i\ \infty+\gamma}^{i\ \infty+\gamma} \frac{(-1+2\ \pi)^{-s}\ \Gamma(-s)^2\ \Gamma(1+s)}{\Gamma(1-s)}\ d\ s\right)^2}{8\ i^2\ \pi^2} +$  $\frac{\left(\int_{-i\,\infty+\gamma}^{i\,\infty+\gamma}\frac{\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,d\,s\right)\int_{-i\,\infty+\gamma}^{i\,\infty+\gamma}\frac{2^{-s}\,\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,d\,s}{2\,i^2\,\pi^2\,\sqrt{2\,\pi}}\,\left(\right)\right)}{for\,-1<\gamma<0$ 

 $\Gamma(x)$  is the gamma function

 $[log base 0.99925625791158988((((2/((2 ln 3 (ln 2/(sqrt(2Pi))) - 2 (ln 3)^2 - (3-1)))))) - (((1/2*0.582879670292435^2 - 0.072815845483680 - (Pi^2)/24 - 1/2(ln((2Pi)))^2))))))) + 11 + 1/golden ratio$ 

# Input interpretation:

$$\log_{0.99925625791158988} \left( \frac{2}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{1}{2} \times 0.582879670292435^2 - 0.072815845483680 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right) + 11 + \frac{1}{\phi} \right)$$

log(x) is the natural logarithm

 $\log_b(x)$  is the base- b logarithm

 $\phi$  is the golden ratio

#### **Result:**

139.61803398875...

139.61803398... result practically equal to the rest mass of Pion meson 139.57 MeV

# Alternative representations:

$$\begin{split} \log_{0.000256257911589880000} \bigg( & 2 \Big/ \bigg( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \bigg( \frac{0.5828796702924350000^2}{2} - \\ & 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) \bigg) + 11 + \frac{1}{\phi} = \\ & 11 + \frac{1}{\phi} + \log \bigg( 2 \Big/ \bigg( -2 \log^2(3) - 2 \bigg( -0.0728158454836800000 + \\ & \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) + \\ & \frac{2 \log(2) \log(3)}{\sqrt{2 \pi}} \bigg) \bigg) \Big/ \log(0.999256257911589880000) \end{split}$$

log<sub>0.999256257911589880000</sub>

$$2 \left/ \left( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \left( \frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \right) \right) \right) + 11 + \frac{1}{\phi} = 11 + \log_{0.55257911589880000} \left( 2 \left/ \left( -2 \log_e^2(3) - 2 \left( -0.0728158454836800000 + \frac{0.5828796702924350000^2}{2} - \frac{\pi^2}{24} - \frac{1}{2} \log_e^2(2 \pi) \right) + \frac{2 \log_e(2) \log_e(3)}{\sqrt{2 \pi}} \right) \right) + \frac{1}{\phi} \right\}$$

$$\begin{split} \log_{0.55256257911589880000} \Biggl( & 2 \Big/ \bigg( \frac{(2 \log(3)) \log(2)}{\sqrt{2 \pi}} - 2 \log^2(3) - (3 - 1) \bigg( \frac{0.5828796702924350000^2}{2} - \\ & 0.072815845483680000 - \frac{\pi^2}{24} - \frac{1}{2} \log^2(2 \pi) \bigg) \Biggr) + 11 + \frac{1}{\phi} = \\ & 11 + \log_{0.55256257911589880000} \bigg( 2 \Big/ \bigg( -2 (\log(a) \log_a(3))^2 - \\ & 2 \bigg( -0.072815845483680000 + \frac{0.5828796702924350000^2}{2} - \\ & \frac{\pi^2}{24} - \frac{1}{2} (\log(a) \log_a(2 \pi))^2 \bigg) + \frac{2 \log^2(a) \log_a(2) \log_a(3)}{\sqrt{2 \pi}} \bigg) \bigg) + \frac{1}{\phi} \end{split}$$

# Series representation:

# **Integral representations:**

(

log<sub>0.</sub>

$$\begin{split} & \frac{2}{\left(\frac{(2\log(3))\log(2)}{\sqrt{2\pi}} - 2\log^2(3) - (3-1)\left(\frac{0.5828796702924350000^2}{2} - 0.0728158454836800000 - \frac{\pi^2}{24} - \frac{1}{2}\log^2(2\pi)\right)\right)\right) + \\ & 11 + \frac{1}{\phi} = \frac{1}{\phi} \left(1 + 11\phi + \phi \log_{0.000256257911589880000} \left(\frac{2}{2} \left(-\frac{\left(\int_{-i\,\omega+\gamma}^{i\,\omega+\gamma}\frac{2^{-5}\,\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,ds\right)^2}{2\,i^2\,\pi^2} - 2\left(0.097058509536428866 - \frac{\pi^2}{24} - \frac{\left(\int_{-i\,\omega+\gamma}^{i\,\omega+\gamma}\frac{(-1+2\pi)^{-5}\,\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,ds\right)^2}{8\,i^2\,\pi^2}\right) + \\ & \frac{\left(\int_{-i\,\omega+\gamma}^{i\,\omega+\gamma}\frac{\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,ds\right)\int_{-i\,\omega+\gamma}^{i\,\omega+\gamma}\frac{2^{-5}\,\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}\,ds}{2\,i^2\,\pi^2\,\sqrt{2\,\pi}}\right) \right) \\ & \text{for } -1 < \gamma < 0 \end{split}$$

 $\Gamma(x)$  is the gamma function

## Appendix

#### **DILATON VALUE CALCULATIONS**

from:

#### Modular equations and approximations to $\pi$ - Srinivasa Ramanujan Quarterly Journal of Mathematics, XLV, 1914, 350 – 372

#### We have that:

5. Since  $G_n$  and  $g_n$  can be expressed as roots of algebraical equations with rational coefficients, the same is true of  $G_n^{24}$  or  $g_n^{24}$ . So let us suppose that

$$1 = ag_n^{-24} - bg_n^{-48} + \cdots,$$

or

$$g_n^{24} = a - bg_n^{-24} + \cdots.$$

But we know that

$$64e^{-\pi\sqrt{n}}g_n^{24} = 1 - 24e^{-\pi\sqrt{n}} + 276e^{-2\pi\sqrt{n}} - \cdots,$$
  

$$64g_n^{24} = e^{\pi\sqrt{n}} - 24 + 276e^{-\pi\sqrt{n}} - \cdots,$$
  

$$64a - 64bg_n^{-24} + \cdots = e^{\pi\sqrt{n}} - 24 + 276e^{-\pi\sqrt{n}} - \cdots,$$
  

$$64a - 4096be^{-\pi\sqrt{n}} + \cdots = e^{\pi\sqrt{n}} - 24 + 276e^{-\pi\sqrt{n}} - \cdots,$$

that is

$$e^{\pi\sqrt{n}} = (64a + 24) - (4096b + 276)e^{-\pi\sqrt{n}} + \cdots$$
(13)

Similarly, if

$$1 = aG_n^{-24} - bG_n^{-48} + \cdots,$$

then

$$e^{\pi\sqrt{n}} = (64a - 24) - (4096b + 276)e^{-\pi\sqrt{n}} + \cdots$$
(14)

From (13) and (14) we can find whether  $e^{\pi\sqrt{n}}$  is very nearly an integer for given values of n, and ascertain also the number of 9's or 0's in the decimal part. But if  $G_n$  and  $g_n$  be simple quadratic surds we may work independently as follows. We have, for example,

$$g_{22} = \sqrt{(1+\sqrt{2})}$$

Hence

$$64g_{22}^{24} = e^{\pi\sqrt{22}} \quad 24 + 276e^{-\pi\sqrt{22}} \cdots,$$
  

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \cdots,$$

so that

$$64(g_{22}^{24}+g_{22}^{-24})=e^{\pi\sqrt{22}}-24+4372e^{-\pi\sqrt{22}}+\cdots=64\{(1+\sqrt{2})^{12}+(1-\sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982\ldots$$

Again

$$G_{37} = (6 + \sqrt{37})^{\frac{1}{4}},$$

$$\begin{array}{rcl} 64G_{37}^{24} & = & e^{\pi\sqrt{37}} + 24 + 276e^{-\pi\sqrt{37}} + \cdots, \\ 64G_{37}^{-24} & = & 4096e^{-\pi\sqrt{37}} - \cdots, \end{array}$$

so that

$$64(G_{37}^{24}+G_{37}^{24})=e^{\pi\sqrt{37}}+24+4372e^{-\pi\sqrt{37}}-\cdots=64\{(6+\sqrt{37})^6+(6-\sqrt{37})^6\}.$$

Hence

$$e^{\pi\sqrt{37}} = 199148647.999978...$$

Similarly, from

$$g_{58} - \sqrt{\left(\frac{5+\sqrt{29}}{2}\right)},$$

we obtain

$$64(g_{58}^{24} + g_{58}^{-24}) = e^{\pi\sqrt{58}} \quad 24 + 4372e^{-\pi\sqrt{58}} + \dots = 64\left\{\left(\frac{5+\sqrt{29}}{2}\right)^{12} + \left(\frac{5-\sqrt{29}}{2}\right)^{12}\right\}.$$

Hence

$$e^{\pi\sqrt{58}} = 24591257751.99999982\dots$$

From:

# An Update on Brane Supersymmetry Breaking

J. Mourad and A. Sagnotti - arXiv:1711.11494v1 [hep-th] 30 Nov 2017

Now, we have that:

From the following vacuum equations:

$$T e^{\gamma_E \phi} = -\frac{\beta_E^{(p)} h^2}{\gamma_E} e^{-2(8-p)C + 2\beta_E^{(p)} \phi}$$

$$16 \, k' e^{-2C} = \frac{h^2 \left(p + 1 - \frac{2\beta_E^{(p)}}{\gamma_E}\right) e^{-2(8-p)C + 2\beta_E^{(p)} \phi}}{(7-p)}$$

$$(A')^2 - k e^{-2A} + \frac{h^2}{16(p+1)} \left(7 - p + \frac{2\beta_E^{(p)}}{\gamma_E}\right) e^{-2(8-p)C + 2\beta_E^{(p)}\phi}$$

We have obtained, from the results almost equals of the equations, putting

4096  $e^{-\pi\sqrt{18}}$  instead of

$$e^{-2(8-p)C+2\beta_E^{(p)}\phi}$$

a new possible mathematical connection between the two exponentials. Thence, also the values concerning p, C,  $\beta_E$  and  $\phi$  correspond to the exponents of e (i.e. of exp). Thence we obtain for p = 5 and  $\beta_E = 1/2$ :

$$e^{-6C+\phi} = 4096e^{-\pi\sqrt{18}}$$

Therefore with respect to the exponential of the vacuum equation, the Ramanujan's exponential has a coefficient of 4096 which is equal to  $64^2$ , while  $-6C+\phi$  is equal to  $\pi\sqrt{18}$ . From this it follows that it is possible to establish mathematically, the dilaton value.

phi = -Pi\*sqrt(18) + 6C, for C = 1, we obtain:

exp((-Pi\*sqrt(18))

Input:  $\exp(-\pi\sqrt{18})$ 

# **Exact result:**

e<sup>-3√2</sup>л

#### **Decimal approximation:**

 $1.6272016226072509292942156739117979541838581136954016...\times 10^{-6}$ 

 $1.6272016...*10^{-6}$ 

Now:

$$e^{-6C+\phi} = 4096e^{-\pi\sqrt{18}}$$

$$e^{-\pi\sqrt{18}} = 1.6272016... * 10^{-6}$$

$$\frac{1}{4096}e^{-6C+\phi} = 1.6272016... * 10^{-6}$$

$$0.000244140625 e^{-6C+\phi} = e^{-\pi\sqrt{18}} = 1.6272016... * 10^{-6}$$

$$\ln(e^{-\pi\sqrt{18}}) = -13.328648814475 = -\pi\sqrt{18}$$

(1.6272016\* 10^-6) \*1/ (0.000244140625)

# Input interpretation: 1.6272016 1

 $\frac{1.6272016}{10^6} \times \frac{1}{0.000244140625}$ 

# **Result:**

0.0066650177536 0.006665017...

 $0.000244140625 \ e^{-6C+\phi} = e^{-\pi\sqrt{18}}$ 

Dividing both sides by 0.000244140625, we obtain:

 $\frac{0.000244140625}{0.000244140625}e^{-6C+\phi} = \frac{1}{0.000244140625}e^{-\pi\sqrt{18}}$ 

 $e^{-6C+\phi} = 0.0066650177536$ 

((((exp((-Pi\*sqrt(18))))))\*1/0.000244140625

# Input interpretation:

 $\exp(-\pi\sqrt{18}) \times \frac{1}{0.000244140625}$ 

#### **Result:**

0.00666501785...

0.00666501785...

 $e^{-6C+\phi} = 0.0066650177536$ 

 $\exp\left(-\pi\sqrt{18}\right) \times \frac{1}{0.000244140625} =$ 

 $e^{-\pi\sqrt{18}}\times \frac{1}{0.000244140625}$ 

= 0.00666501785...

ln(0.00666501784619)

# Input interpretation:

log(0.00666501784619)

# **Result:**

-5.010882647757...

-5.010882647757...

Now:

 $-6C + \phi = -5.010882647757 \dots$ 

For C = 1, we obtain:

 $\phi = -5.010882647757 + 6 = 0.989117352243 = \phi$ 

#### **Observations**

All the results of the most important connections are signed in blue throughout the drafting of the paper. We highlight as in the development of the various equations we use always the constants  $\pi$ ,  $\phi$ ,  $1/\phi$ , the Fibonacci and Lucas numbers, linked to the golden ratio, that play a fundamental role in the development, and therefore, in the final results of the analyzed expressions.

In mathematics, the **Fibonacci numbers**, commonly denoted  $F_n$ , form a sequence, called the **Fibonacci sequence**, such that each number is the sum of the two preceding ones, starting from 0 and 1. Fibonacci numbers are strongly related to the golden ratio: Binet's formula expresses the *n*th Fibonacci number in terms of *n* and the golden ratio, and implies that the ratio of two consecutive Fibonacci numbers tends to the golden ratio as *n* increases.

Fibonacci numbers are also closely related to Lucas numbers in that the Fibonacci and Lucas numbers form a complementary pair of Lucas sequences

The beginning of the sequence is thus:

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, 2584, 4181, 6765, 10946, 17711, 28657, 46368, 75025, 121393, 196418, 317811, 514229, 832040, 1346269, 2178309, 3524578, 5702887, 9227465, 14930352, 24157817, 39088169, 63245986, 102334155...

The Lucas numbers or Lucas series are an integer sequence named after the mathematician François Édouard Anatole Lucas (1842–91), who studied both that sequence and the closely related Fibonacci numbers. Lucas numbers and Fibonacci numbers form complementary instances of Lucas sequences.

The Lucas sequence has the same recursive relationship as the Fibonacci sequence, where each term is the sum of the two previous terms, but with different starting values. This produces a sequence where the ratios of successive terms approach the golden ratio, and in fact the terms themselves are roundings of integer powers of the golden ratio.<sup>[1]</sup> The sequence also has a variety of relationships with the Fibonacci numbers, like the fact that adding any two Fibonacci numbers two terms apart in the Fibonacci sequence results in the Lucas number in between.

The sequence of Lucas numbers is:

2, 1, 3, 4, 7, 11, 18, 29, 47, 76, 123, 199, 322, 521, 843, 1364, 2207, 3571, 5778, 9349, 15127, 24476, 39603, 64079, 103682, 167761, 271443, 439204, 710647, 1149851, 1860498, 3010349, 4870847, 7881196, 12752043, 20633239, 33385282, 54018521, 87403803.....

All Fibonacci-like integer sequences appear in shifted form as a row of the Wythoff array; the Fibonacci sequence itself is the first row and the Lucas sequence is the second row. Also like all Fibonacci-like integer sequences, the ratio between two consecutive Lucas numbers converges to the golden ratio.

A Lucas prime is a Lucas number that is prime. The first few Lucas primes are:

2, 3, 7, 11, 29, 47, 199, 521, 2207, 3571, 9349, 3010349, 54018521, 370248451, 6643838879, ... (sequence A005479 in the OEIS).

In geometry, a **golden spiral** is a logarithmic spiral whose growth factor is  $\varphi$ , the golden ratio.<sup>[1]</sup> That is, a golden spiral gets wider (or further from its origin) by a factor of  $\varphi$  for every quarter turn it makes. Approximate logarithmic spirals can occur in nature, for example the arms of spiral galaxies<sup>[3]</sup> - golden spirals are one special case of these logarithmic spirals

# References

# A Reissner-Nordstrom+Λ black hole in the Friedman-Robertson-Walker

universe- arXiv:1703.05119v1 [physics.gen-ph] 5 Mar 2017 Safiqul Islam and Priti Mishra<sup>†</sup> Harish-Chandra Research Institute, Allahabad 211019, Uttar Pradesh, India Homi Bhabha National Institute, Anushaktinagar, Mumbai 400094, India Farook Rahaman<sup>‡</sup> Department of Mathematics,Jadavpur University,Kolkata-700 032,West Bengal,India - (Dated: March 16, 2017)

### Generating functions of wormholes

arXiv:1901.01757v1 [physics.gen-ph] 1 Jan 2019

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#### Manuscript Book 2 of Srinivasa Ramanujan