# On the Nature and Origin of Dark Energy, Cosmological Constant and Dark Matter

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#### Abstract

In the present essay, we consider the origin of the dark energy, cosmological constant and the dark matter. The dark energy, is consequence of the annihilation of the matter - antimatter at the very biginning of the big bang. This dark energy was the origin and cause of the cosmological expansion and the past and present creation of the whole space. We consider the presence of the call "dark" matter as consequence of highly exited hydrogen and helium Ridberg's atoms in perfect equilibrium with the CMB radiation. The cosmological constant is considered as an arbitrary ad hoc anti-gravitational entity. Finally, we consider the Casimir effect, as a suitable and truly efficient physical method and a reliable resource in the experimental determination of the dark energy.

**Keywords:** Cosmology; Dark Matter; Dark Energy; Empty space, Casimir effect; Rydberg atoms; Hubble constant; CMB radiation.

#### 1 Introduction

Nature always has the same design, which evolved from simple elementary units to produce more complex structures. In cosmology and astrophysics all its evolutionary processes was originated from a plasm of gas formed principally by ions, free electrons, neutrinos and radiation.

As the intensity of the electrical force is 10<sup>39</sup> times stronger than the gravitational interactions, during the recombination the electrical charge are canceled and lather the gravitational collapse is produced in the formation of the massive structures as galaxies and stars. In consequence, the characteristics of all these structures - including all the minior unities - were imposed and established by the hegemonic arrangement of the whole. The Rydberg H and He highly excited atoms are the best candidates in the formation of the called "dark matter". This Rydberg atoms, from the recombination they are in perfect equilibrium with the CMB radiation, and do no interacts with any other shorter forms of the electromagnetic radiation i.e. UV, IR, X, gamma. However, this Rydberg's atoms together with the "ordinary" matter were fundamental in the formation of galaxies and stars. The evidence of his presence is noted in the anomalous rotation curves of spiral galaxies. Also, the observation of the phenomenon called "gravitational lensing" between galaxies and cumulus of galaxies can be only attributed to the "dark" matter (Zwicky, F. 1937). All this gravitational "anomalies" can be perfectly caused by the highly excited H and He Rydberg atoms.

The empty cosmological space is all "dark" energy. The source of this energy was originated from the initial conditions of the big bang process whose physical significance is related as the expansive evolution of the space. This process was initiated from the annihilation of near the same matter - antimatter particles. At the present time development, the empty space energy density is the same as the registered by the Casimir effect.

# 2 Microspace vacuum and macrospace vacuum

#### 2.1 Relativistic meaning of the spectral lines

For an electron pertaining to an isolated hydrogen atom, when n = 1 and v = c/137 ( $v \ll c$ ), the Lorentz relativistic expression may by stated in the following form

$$m_0(1+\delta) = m_0 \left(1 + \frac{v^2}{c^2}\right)^{1/2} \simeq m_0 \left(1 + \frac{v^2}{2c^2}\right)$$
 (1)

When this single electron evolves from a state (i) towards a state (j), there is within the empty contour of the atom a mass increase of  $\Delta m$ 

$$m_i = m_e \left( 1 + \delta_i \right) \tag{2}$$

$$m_j = m_e \left( 1 + \delta_j \right) \tag{3}$$

$$\Delta m = m_i - m_j = m_e \left( \delta_i - \delta_j \right) \tag{4}$$

Taking into account  $\delta = v^2/c^2 = \alpha^2/n^2$ , being  $\alpha$  the Sommerfeld constant, and as this relationship expresses the relativistic quantum ratio in electromagnetic emission (or absorption), we can insert it in (1) and (4)

$$\Delta m = m_e \left( \frac{v_i^2}{2c^2} - \frac{v_j^2}{2c^2} \right) = \frac{m_e \alpha^2}{2} \left( \frac{1}{n_i^2} - \frac{1}{n_j^2} \right)$$
 (5)

Since  $\alpha = e^2/\hbar c$ , we have

$$\Delta m = \frac{m_e e^4}{2\hbar^2 c^2} \left( \frac{1}{n_i^2} - \frac{1}{n_i^2} \right) \tag{6}$$

As with the expansion, the kinetic energy K diminishes and the potential energy U increases, this means that the potential energy is equivalent to the space<sup>1</sup> that has been created. Likewise, the spectral process of emission or absorption is an interaction between a microbubble of energy (atom) and the macrospace. In this process, both entities always exchange simultaneously the same quantum unit of energy. The absorption lines expresses the mass-energy quantity proceeding from the exterior space, and the emission lines are equivalent to the mass-energy transferred to the macrospace when the electron falls down to an inferior quantum level.

This correlativity of mass-energy and space-time reciprocal exchange is the foundation for establishing the equivalence between both vacuum contours: the microspace "vacuum" mass-energy and the macrospace "vacuum" mass-energy (Section 2.2).

From the Equations (1) and (6) it is evident that as the atomic radius increases, the electron energy decreases and  $\Delta m$ , which means the mass equivalent of the empty atomic space between  $n_i$  and  $n_j$  increases too.

Likewise, according to Bohr's formalism, the electron "velocity" is  $v_i$  for  $n_i = 1$  and  $r_i = a_0$  (Bohr radius). When the atom is excited or "expands", v decreases inversely and linearly in terms of the Bohr's radius:  $v = \hbar/(m_e n a_0)$ .

<sup>&</sup>lt;sup>1</sup>The space is equivalent to mass or energy

As the velocity depression is also parametrized with respect to a scale unit  $(a_0)$ , it allows us to establish the following formalism:

$$\frac{v_j}{v_i} = \frac{a_0}{r_j} = \frac{1}{n_j^2} \tag{7}$$

#### 2.2 Cosmological expansion and the hydrogen atom excitation

According to Eq.(7) it may be deduced that the relativistic mass of a photon emitted or absorbed for any transition is inversely proportional to the ratios of the corresponding stable orbits.

Consequently

$$\frac{m_i}{m_j} = \frac{r_j}{a_0}, \qquad r_j = 4a_0, 9a_0, \dots, n^2 a_0$$
 (8)

Also the following proportions are valid:

$$\frac{m_i}{m_j} = \frac{E_i}{E_j} = \frac{T_i}{T_j} = \frac{r_j}{a_0} = \frac{n_j^2}{n_i^2} = \frac{\lambda_j}{\lambda_i}$$
(9)

This means, that the relativistic interactive photons mass-energy is directly proportional to the relativist temperature, and inversely proportional to the atomic radius. Even though it is certain that the expansion of the Universe operates in a continuous form, it is a particular congruence that the information of the event was provided by quantum transitions of atomic emissions systems. If for a practical convenience, we change the sign of these transitions, and instead of emission, it would correspond to the excitement of an electron of an isolated hydrogen atom. Here, its eigenvalues would have the same scale proportions in their spatial development as the cosmological values expressed as redshift or temperature of the CMB radiation.

This correspondence, is due to the equivalence between the energetic mechanism itself that originates the radiation (quantum states) associated to the size of the atoms its emitted wavelength, and the size of the Universe in expansion.

It is because of that

$$z + 1 = \frac{\lambda_{obs}}{\lambda_{em}} = \frac{R_U^0}{R_{em}} = \frac{n_j^2}{n_i^2} = \frac{T_{em}}{T_{obs}}$$
 (10)

Where z is the measurement of the cosmological expansion;  $R_{em}$  and  $R_U^0$  are the respective Universes radii when light was emitted, compared with the present radius.

For a transition  $n_i = 1$  to  $n_j = 2$ , the atomic radius is 4 times greater,  $\lambda_{obs}$  for n = 2 is 4 times larger too. If z = 3, it means that the Universe was 4 times smaller  $R_{em} = R_u^0/4$ , or what is the same, the wavelength emitted was a quarter of the observed  $\lambda_{em} = \lambda_{obs}/4$ .

As the monodimensional parameters of cosmological expansion have the same ratio as those of atomic excitation states, it means that the energetic implications of both vacuum contours are identical, despite of their scale magnitudes.

Thus, due to the cosmological expansion, the Lyman alpha line shift of the atomic hydrogen spectra, coincides with the ratio between the two atomic radii which generates this transition Eq. (10). E.g., for z=3 the Lyman alpha line is shifted to a cosmological expansion with a factor 4. Likewise, when an isolated hydrogen atom originates a photon of  $\lambda=1,216\mathring{A}$ , the electron has a quantum transition from  $n_j=2$  to  $n_i=1$ , due to a spatial transition of  $4a_0\to a_0$ . Although we have adopted the intense Lyman alpha line, the same properties for any other electronic transition can be verified.

#### 2.3 Macrocosm and microcosm moments of interaction

I view of these preliminary antecedents of equivalence - which link the gravitational field with the Coulombic field - it is possible to relate the atomic and subatomic universe, to the cosmological Universe. In order to accomplish this, we will connect both scales through their corresponding moments of interaction (Law of the Lever). Then, the moment between the microscopic and macroscopic magnitudes can be made equal and be superimposed in the following way:

Energy A = Energy B
$$F_G \times L_{max} = F_{coul} \times r_e$$
(11)

The "classical electron radius"  $r_e$ , physically has an entirely relativistic signification of equivalence between mass, radial distance and the unit of charge. This constant  $r_e$ , is the radial separation between two electrical charges when the Coulombic potential of energy is equivalent to the electron relativistic mass  $m_e c^2 = e^2/r_e$ . The gravitational interaction between a proton and an electron in the in the domain of  $r_e$  is  $F_G = Gm_p m_e/(2\pi^2 r_e^2)$ . As in this conditions  $F_{coul} = e^2/r_e^2 = m_e c^2/r_e$  we can substitute it in the Eq. (11) and resolve for  $L_{max}$ .

$$L_{max} = \frac{2\pi^2 r_e e^2}{Gm_p m_e} = \frac{2\pi^2 r_e^2 c^2}{Gm_p} = 1.26 \times 10^{28} cm = 1.36 \times 10^{10} Ly$$
 (12)

Being:  $L_{max}$  Universe critical radius; electron charge  $e = 4.8 \times 10^{-10} cm^{3/2} g^{1/2} s^{-1}$ ; electron mass  $m_e = 9.11 \times 10^{-28} g$ ; proton mass  $m_p = 1.673 \times 10^{-24} g$ ; gravitational constant  $G = 6.67 \times 10^{-8} cm^3 g^{-1} s^{-2}$ ; classical radius  $r_e = 2.82 \times 10^{-13}$  cm.

It is evident the critical radius  $L_{max}$  established in this way is a constant, because it was originated by means of constants. Nevertheless, as  $L_{max}$  is a superior limit, it is accomplished when the expansive energy is the same as the potential energy. As the generalized state of expansion continues, this limit in the present has not been reached.

#### 2.4 Critical number of protons

A microspace contour, and all the whole Universe contour are complementary when these opposite extremes are represented by means of a limited energy bubble with a well defined critical radius in its spherical surface. This makes it possible to determine another critical parameter, which can be found applying the Principle of Correspondence (Bohr, 1929) about Eq.(12). Its result lead to the obtainment of the number of baryons  $N_b$  and the critical mass  $m_U^0$ .

Multiplying and dividing Eq. (12) by N, being N a constant

$$L_{max} = \frac{2\pi^2 r_e^2 N c^2}{Gm_p N} = \frac{R_U^2 c^2}{2Gm_U^0}$$
(13)

as 
$$m_U^0 = m_p N_b$$
 and  $L_{max}^2 = 4\pi^2 r_e^2 N_b$  (14)

from which we obtain the Schwartzchild Radius <sup>2</sup>.

$$L_{max} = \frac{2GM}{c^2}; \quad M = m_U^0 \tag{15}$$

<sup>&</sup>lt;sup>2</sup>The scale  $4.10 \times 10^{17}$ s:  $1.23 \times 10^{28}$ cm:  $8.36 \times 10^{55}$ g, is the same as Schwartzchild scale in Natural Units 1s:  $3 \times 10^{10}$ cm:  $2 \times 10^{38}$ g.

The equations (13) and (14) show that  $N_b$  represent the critical number of baryons. Therefore:

$$N_b = \left(\frac{L_{max}}{2\pi r_e}\right)^2 = \left(\frac{\pi r_e c^2}{G m_p}\right)^2 = \left(\frac{\pi e^2}{G m_p m_e}\right)^2 = 5.08 \times 10^{79}$$
 (16)

The critical baryon density is:

$$\rho_b = \frac{3N_b m_p}{4\pi R_U^3} = \frac{3}{4\pi} N_b m_p \left(\frac{H_0}{c}\right)^3 = 1.09 \times 10^{-29} g \cdot cm^3 \tag{17}$$

The Principle of Correspondence is clearly expressed in the Eq.(16) when microphysics scale gets connected with cosmological scale through the  $N_b$  constant.

The ratio of interaction between two units of charges, with respect to the intensity of its gravitational field is  $7.13 \times 10^{39}$  times greater. It signifies that  $7.13 \times 10^{39}$  units of mass are required to produce a gravitational field of the same intensity as a single pair of units of charge. These assertion and principles can be applied to other very extensives or massive forms: galaxies formation, the structure of the Sun and stars.

#### 3 The Hubble constant

#### 3.1 Kinematics implications of $H_0$

Theorically, the Hubble constant is defined as a parameter established by the speed of the cosmological expansion within a scale unit (Misner *et al*; 1972).

$$H = \frac{\dot{R}}{R}$$

Starting from this constant, the following parameters can be deduced: a) Linear recession law:  $v = dl/dt = \dot{l} = \dot{R}l/R$  being l, the mean distance between two referential physical points (i.e. galaxies). b) Hubble time  $t_H = l/v = H^{-1}$  where  $t_H$  is the time from the present referential position, extrapolated to zero distance between galaxies moving at the recession rate observed today. c) Hubble length  $L_H = c/H$ , where  $L_H$  is the top distance, which is attained by use of the linear recession law when v is extrapolated to c.

#### 3.2 The origin of $H_0$

One microsecond of parallax (parsec), given by the diameter of the terrestrial orbit around the Sun, is an anthropic scale unit, and physically unmeaning by itself. The origin of  $H_0$  must be marked by a physic unit of scale transcendent and significant as the radius of the gravitational collapse  $R_G$ , which it may allow us the acquisitions of physical implications which are comparative to the atomic referential radius as unit of scale (i.e.  $a_0$  or  $r_e$ ).

When the Universe radius was  $6.20 \times 10^{24}$  cm =  $2 \,\mathrm{Mps} = R_G$  with a Planck's blackbody distribution curve corresponding to a temperature of  $\sim 5,400^\circ\mathrm{K} = T_G$ , there still existed a fraction of photons in a thermic state equivalent to  $\sim 166,000^\circ\mathrm{K}$ , whose number was the same as the whole population of baryons.

Starting from these conditions, the collapse of gravitation is produced; all the matter and radiation which up to that epoch was in an undifferenciated state of plasm, undergoes a 3-d globular packing condensation. The development of these clumps is a fundamental point of reference: the

history of the cosmological expansion begins with the withdrawal of these formations, in order to mark the initial time of  $H_0^{-1}$ .

Since kilometer and megaparsec are units of distance, the dimensions km s<sup>-1</sup>.Mps<sup>-1</sup> means second<sup>-1</sup>; then, as the cosmological space progresses, the Hubble expansion rate will decrease continuously, until it reaches the present time value of  $H_0 = 75.4 \text{ Km s}^{-1} \text{ Mps}^{-1} = 151 \text{ Km s}^{-1} 2 \text{ Mps}^{-1}$  (Table 1).

At the present the observational determination of  $H_0$  shows acceptable precise values and by means of different methods converges within  $H_0 = 73.8(\pm 3.1) \text{ Km} \cdot \text{s}^{-1} \cdot \text{Mps}^{-1}$  (Riess, 2011);  $H^0 = 73(\pm 2)(\pm 4) \text{ Km} \cdot \text{s}^{-1} \cdot \text{Mps}^{-1}$  (Freedman - Madore, 2010);  $H^0 = 73.9 \text{ Km} \cdot \text{s}^{-1} \cdot \text{Mps}^{-1}$  (Bonamente, 2006);  $H_0 = 76.5 \text{ Km} \cdot \text{s}^{-1} \cdot \text{Mps}^{-1}$  (Holanda, 2011);  $H_0 = 74.3 \text{ Km} \cdot \text{s}^{-1} \cdot \text{Mps}^{-1}(\pm 2.1)$  (Freedman - Madore, 2012).

#### 3.3 Dynamic implications of $H_0$

Taking into account the Cosmological Principle, and considering  $H_0$  for a simultaneous time (unobservable) for any point in all the extension of the space, we may establish the dynamic state of the Universe from the radiative transition, to baryonic up to present time. Thus, for the extremes  $R_G = 2$  Mps (gravitational collapse) and  $R_U^0$  (present time radius) we have

$$H_0 = \frac{c}{(z+1)R_G} = \frac{2v}{R_G} = 2.45 \times 10^{-18} \,\mathrm{s}^{-1} \tag{18}$$

being  $v = 7.6 \times 10^6 \, \mathrm{cm \, s^{-1}}$  ;  $R_G = 6.20 \times 10^{24} \, \mathrm{cm}$ 

Also: 
$$H_0 = \frac{c}{R_U^0} = 2.45 \times 10^{-18} \text{ s}^{-1}$$
 (19)

where  $R_U^0 = 1.225 \times 10^{28} \text{cm}$ 

Equalizing (18) with (19) and reordering, we find the following dimensionless scale

$$\frac{2v}{c} = \frac{1}{z+1} = \frac{2H_0}{H} = \frac{R_G}{R_U^0} \tag{20}$$

Any value from the linear recession law is comparable to whatever intensive property of a system i.e. it is similar to the absolute temperature used universally as an indicator of the thermic state, or as a measure of energy for any system.

Then

$$\frac{2v}{c} = \frac{T}{T_G} \qquad T_G: \text{ Gravitational collapse temperature}$$
 (21)

Since  $H_0$  defines the present Hubble expansion rate, and H defines a value of the Hubble constant at different epoch, we may extend (20) in the following way:

$$\frac{2v}{c} = \frac{1}{z+1} = \frac{2H_0}{H} = \frac{R_G}{R_U} = \frac{T}{T_G} = \left(\frac{8m_V}{M_V}\right)^{1/2} \tag{22}$$

 $M_V = 2.64 \times 10^{63}$ g is the mass of the cosmological vacuum (Sect. 4.3). Raising to square all this dimensionless terms and reordering, we find

$$m_V = \frac{M_V v^2}{2 c^2} = \frac{M_V}{8 (z+1)^2} = \frac{M_V H_0^2}{2 H^2} = \frac{M_V R_G^2}{8 R_U^2} = \frac{M_V T^2}{8 T_G^2}$$
(23)

These proportions express the dynamic state of the Universe unquestionably. The term  $M_V v^2/2 c^2$ , the same as the other terms, represents the relativistic vacuum  $m_V$  mass-energy equivalence of the space in expansion.

Despite of the different methods for the determination of the Hubble constant, and the implications of the Universe age, for us,  $H_0^{-1}$  as well as  $t_0$ , are not independent quantities, since we consider for  $H_0$  a clear point of arribal. Thus  $R_G = 2$  Mps  $(6.20 \times 10^{24} \text{ cm})$  referential point, is coincident with the initial withdrawal of the gas protogalaxies after gravitational collapses.

The Hubble time is an indicator of the cosmological age through the expansion rate in relation with the  $R_G$  referential point of departure. Hence, the present value of  $H_0^{-1}$  means the duration of the expansion from  $R_G$  until now. For this reason,  $t_0 = \text{age}$ , determined on the basis of the antiquity of the oldest objects, plus its time of formation, is the same as  $t_0 \simeq H_0^{-1}$ , as likewise  $H_0 t_0 \simeq 1$ .

#### 4 The extension of the cosmological space

#### 4.1 Energy constraint

All terms of the Eq.(23) determine the main implication of the Hubble parameter, because it establishes the dynamic index (scale factor) of the relativistic kinetic energy of the global expansion, prevailing for any point in space in a simultaneous time (Cosmological Principle).

In the initial evolutive process, because of  $E_V > E_G$  and  $m_V > m_M$ , the Universe was hegemoneously expansive. Up to the  $R_G \sim 2$ Mps, the gravitation collapses, and as it implies a force exerted, this makes a continuous decrease of  $m_V = M_V v^2 / 2 c^2$ . Thus, the space expansion range can be established by means of the ratio between the expansive energy and the gravitational attractive force (Planck, 1926).

Slightly modifying the mechanical equivalent of heat, we have:

Expansive energy = 
$$F_{\text{grav}}L_{\text{max}}$$
 (24)

As  $F_{\text{grav}}L_{\text{max}}$  is the potential energy U, it determines that the expansive energy (kinetic K) be depressed continuously up to the equilibrium limit given by  $\frac{1}{2}K = U$ , which constraints the Universe extension  $(L_{\text{max}})$ .

$$L_{\text{max}} = \frac{M_V v^2}{2 G m_U^{0.2}} R_U^2 \tag{25}$$

 $m_U^0$ : critical mass =  $N_b m_p$ (constant)

Being  $N_b = 5 \times 10^{79}$ ;  $m_U^0 = 8.35 \times 10^{55}$  g and  $M_V$ : mass of the vacuum  $2.64 \times 10^{63}$ g (Sect. 4.3),  $K = m_\Lambda = M_V v^2 / 2 c^2$  (dynamic mass of the vacuum) and  $U = m_M = 2 \, G m_U^{0.2} / c^2 R_U$  (gravitational mass).

Considering  $R_G$  as the starting point, for any historic value of  $R_U$  and v, the results from Eq. (25) are always  $L = 1.23 \times 10^{28} \text{cm} = 1.32 \times 10^{10} \text{ly}$ .

#### 4.2 Physical meaning of the cosmological term

The cosmological constant  $\Lambda$ , was designed exclusively for static model of universe. Its origin, was from an arbitrary *ad-hoc* constant of integration (Peebles P.J.E. 1993), and its negative sign, gives it the meaning of a repulsive "*antigravity*". Because of its static non-expansive nature, its

implementation is ineffective for any previous stage in the evolution of the universe. Moreover, this repulsive term acts only on the space itself, but not acting on the matter. For this properties, it does not gravitates.

As a consequence of its static origin, the Eq.(25) is used with all terms as constants

$$L_{\text{max}} = \frac{M_V v^2}{2Gm_U^{0.2}} R_U^2$$

Multiplying both terms by  $\frac{4\pi R_U c^2}{3}$  and reordering

$$\frac{3c^2}{8\pi R_U L_{\text{max}}} = \frac{2 G \rho_{m_U^0} m_U^0 c^2}{M_V v^2} \qquad \text{Being } \rho_{m_U^0} = \frac{3m_U^0}{4\pi R_U^3} \simeq \rho_{\Lambda} = \rho_V$$
 (26)

At present time  $R_U^0 \simeq L_{\text{max}}$ , and  $m_U^0 \simeq m_V \simeq m_\Lambda \simeq \frac{M_V v^2}{2 c^2}$ . Then

$$\Lambda = \frac{1}{L_{\text{max}}^2} = \frac{-8\pi}{3c^2} G \, \rho_{\Lambda} \simeq \frac{8\pi}{3c^2} G \, \rho_{m_U^0} \tag{27}$$

As  $c^2/L_{max}^2 \simeq H_0^2$ 

$$H_0^2 = \frac{-8\pi \, G \, \rho_\Lambda}{3} \simeq \frac{8\pi \, G \, \rho_{m_U^0}}{3} \tag{28}$$

For  $H_0 = 2.44 \times 10^{-18} \text{s}^{-1}$ ;  $\rho_{\Lambda} = 1.10 \times 10^{-29} \text{g cm}^{-3}$ 

This means definitely, that the origin of the cosmological constant proceed from the referential energy of the vacuum  $m_V$  (Eq. 23).

It is very evident that the cosmological constant  $\Lambda$  do no shows evolution; it not has pass or future: it is totally adjusted to the present time. Clearly it states that the cosmological constant is directly imposed by the present critical mass.

After the discovery of the expansive universe by Hubble, the cosmological constant was abandoned, and Einstein himself considered it as the worst *schlupfen* (blunder) of his life.

However, in the last 25 years, the cosmological constant was retaken and currently is considered as the greatest star than shines in the sky of the standard model of cosmology.

#### 4.3 Origin and evolution of the repulsive dark energy

All the photons of the CMB radiation vibrate in all possible directions through a symmetric axis. But, as they have their origin in the annihilation of almost the same quantity of matter-antimatter, they are formed from  $N_{\gamma}/2$  pairs of polarized waves. This polarization still remains after the inverse thermoionization (recombination) because the recombinant electron also collapses in atoms with two possible quantum states. Likewise, the electrons of the hydrogen atoms and He too, show two equal quantum states and emit polarized photons in both pairs.

Because the great supremacy of the  $N_{\gamma}/2$  pairs of polarized waves, and despite of the perturbations provoked by the  $N_{\rm b}$  baryons, this scheme remains invariant through all the cosmological evolution. Therefore, from the present conditions, if we fix an inverse sequential order towards a collapse on the space itself (gravitational implosion), it will show the following phases:

a - When the temperature is higher than 4,000°K the electrons and the hydrogen and helium nucleus will still be at the plasma state. The  $N_{\gamma}$  photons of the CMB radiation keep their polarity, taking into account that they are  $1/2N_{\gamma}(-)$  and  $1/2N_{\gamma}(+)$ .

- b For the electrons' threshold temperature  $T\sim 6\times 10^{9}\,\mathrm{c}$ K and  $R_U\sim 2.6\times 10^{19}\,\mathrm{cm},\,1/4$  photons (-) and 1/4 photons (+) collapses as 1/4 electrons and 1/4 positrons.
- c When  $R_U \sim 1.6 \times 10^{16}$  cm and  $T > 2 \times 10^{12}$ °K (neutron's threshold temperature) other 1/4 photons (+) plus 1/4 photons (-) collapse as 1/4 protons and 1/4 antiprotons, their final result being N/2 neutrons.  $\left\{ \begin{array}{l} 1/4N(p^+ + e^- + \nu_{\rm neutrino} \to n^0) \\ 1/4N(p^- + e^+ + \nu_{\rm antineutrino} \to n^0) \end{array} \right\} N/2 \text{ neutrons}$  Where  $N/2 = 1.6 \times 10^{87}$  neutrons, and the constant  $\underline{M_V} = 2.6 \times 10^{63} \, \mathrm{g}$  is the mass intake from the empty space.
- d Finally, this N/2 neutrons coalesces to give  $\sim 1.2 \times 10^{68}$  Planck's "particles" when  $R_U = 6.4 \times 10^{-11}$  cm and  $T = 1.62 \times 10^{32}$  °K.

In a cyclic, or periodic Universe, the Planck state was not an initial ex-nihilo big bang starting point, instead, it was a crossing point for a new cycle. As at this point, there is not a preexistent surface, the Universe does not rebound on it, but it passes across itself, and expands toward any 3d points of space. Then, the former inward gravitational implosive falling energy was shifted to an opposite outward acceleration. This accelerative expansion, in fact, was not simultaneously canceled by an equal attractive gravitational field (g=0). Consequently, the origin of the cosmological expansion was produced exclusively from matter-antimatter annihilation (dark energy).

Both opposite interactions were still unchanged until the gravitational baryonic collapse, which started at 2Mps (Sect. 3.2).

#### 4.4 Photons number density of the CMB radiation

The energy spectrum of the CMB radiation registered at present, whose mean wavelength is 0.105 cm, represents a huge magnified copy of the photons produced by annihilation of  $m_p^{\pm}$  and  $m_e^{\pm}$  (matter - antimatter particles). The number of photons  $\eta_{\gamma}$  of the CMB radiation per cm<sup>-3</sup> may be easily calculated from the Wien's Law.

$$T \cdot \lambda_{CMB} = \frac{2\pi \hbar c}{5k}$$
 Reordering  $\frac{2\pi}{5\lambda_{CMB}} (cm^{-1}) = \frac{kT}{\hbar c} (cm^{-1})$  (29)

In order to obtain it, is only necessary to apply in both terms the sphere formula:

$$\eta_{\gamma} = \frac{6\pi^2 \,\text{cm}^{-3}}{(5\lambda_{CMB})^3} = \frac{3}{4\pi} \left(\frac{k \, T_{CMB}}{\hbar \, c}\right)^3 \,\text{cm}^{-3} = 19.8^{\circ} \text{K}^{-3} cm^{-3} T^3$$
 (30)

e.g.  $T_{CMB} = 2.73$ °K and  $\lambda_{CMB} = 0.105$ cm;  $\eta_{\gamma} = 404$  photons·cm<sup>-3</sup>.

Otherwise, the Universe photons number  $N_{\gamma}$  is a constant of nature since  $T_{CMB} \cdot R_U$  and  $R_U/\lambda_{CMB}$  are constants:

$$N_{\gamma} = \left(\frac{2\pi R_U}{5\lambda_{CMB}}\right)^3 = \left(\frac{k T_{CMB} R_U}{\hbar c}\right)^3 = 3.12 \times 10^{87}$$
 (31)

This equality shows the invariance of  $N_{\gamma}$  throughout the evolution of  $R_U$ . Multiplying the Eq. (30) by  $kT/c^2$ , we can arrive to the Universe density of the CMB radiation in g·cm<sup>-3</sup>.

$$\rho_{CMB} = \frac{3}{4\pi} \frac{\left(kT_{CMB}\right)^4}{\hbar^3 c^5} = 3.00 \times 10^{-36} g \, cm^{-3} \, \text{e}^{-3} \, \text{K}^{-4} T^4$$
(32)

Clearly in the expansion process from a temperature of  $2 \times 10^9$  °K to 2.73 °K, a huge transfer of energy to the own created space is produced.

#### 4.5 Dynamic repulsive density of the empty space

Because of its expansive origin (from annihilation of matter-antimatter particles) the cosmological vacuum is a repulsive "antigravitational" entity. Then, at the present temperature of the CMB radiation (2.73 °K), the vacuum density of energy is equivalent to

$$\rho_{vac} = 102 \left( m_p^+ + m_p^- + m_e^- + m_e^+ \right) \cdot c^2 = 204 m_p^{\pm} \cdot c^2 = 0.31 \text{ erg} \cdot \text{cm}^{-3}$$
Since:  $\left( m_p^+ + m_p^- \right) \simeq m_p^{\pm} \text{ and } 204 = \frac{1}{2}408$ 

From Eq. (30) the static vacuum energy density at any temperature below  $1 \times 10^{9}$ °K is

$$\rho_{vac} = \frac{1}{2} \eta_{\gamma} \cdot m_p^{\pm} \cdot c^2 \text{ and } \rho_{vac} = \frac{3m_p^{\pm}}{8\pi c} \left(\frac{kT}{\hbar}\right)^3 = 0.015 \text{ erg} \cdot \text{cm}^{-3} \cdot {}^{\circ}\text{K}^{-3} \cdot T^3$$
(33)

After the gravitational collapse, at temperature bellow 5,400  $^{\circ}$ K, the vacuum dynamical density in g·cm<sup>-3</sup> is:

$$\rho_V = \frac{3m_p^{\pm} \cdot v^2}{16\pi c^2} \left(\frac{kT}{\hbar c}\right)^3 = 5.29 \times 10^{-31} g \, \text{cm}^{-3} \, \text{K}^{-3} T^3$$
 (34)

As the temperature  $T_G = 5,400^{\circ}$ K marks a point of departure from the gravitational collapse, by use of the Eq.(21), we have:

$$\rho_V = \frac{3m_p^{\pm} \cdot T_{CMB}^5}{64\pi T_G^2} \left(\frac{k}{\hbar c}\right)^3 = 7.10 \times 10^{-32} \text{ g} \cdot \text{cm}^{-3} \cdot {}^{\circ}\text{K}^{-5} \cdot T^5$$
 (35)

At the present time  $T = T_{CMB}$ , radiation = 2.73°K and  $\rho_V = 1.08 \times 10^{-29} g \, cm^{-3}$ .

Time	Temp.	$R_U$	~	$ ho_b$	$ ho_V$	$ ho_{CMB}$	$_{ m H}$	H	
seg.	$^{\circ}\mathrm{K}$	$^{ m cm}$	z	$g \cdot cm^{-3}$	$\mathrm{g}\cdot\mathrm{cm}^{-3}$	$g \cdot cm^{-3}$	${\rm Km \cdot s^{-1}} \ R_G^{-1}$	$\mathrm{Km}\cdot\mathrm{s}^{-1}\ \mathrm{Mps}^{-1}$	
$2.13 \times 10^{14}$	5,400	$6.20 \times 10^{24}$ *	2,000	$8.96 \times 10^{-20}$	$3.25 \times 10^{-13}$	$2.55 \times 10^{-21}$	$3.0 \times 10^{5}$	$1.50 \times 10^{5}$	
$3.34 \times 10^{14}$	3,350	$1.01 \times 10^{25}$	1,280	$1.97 \times 10^{-20}$	$3.00 \times 10^{-14}$	$3.82 \times 10^{-22}$	$2.0 \times 10^{5}$	$9.69 \times 10^{4}$	
$4.27\times10^{14}$	2,625	$1.28 \times 10^{25}$	960	$9.68 \times 10^{-21}$	$8.85 \times 10^{-15}$	$1.44 \times 10^{-22}$	$3.0 \times 10^{4}$	$1.45 \times 10^{4}$	
_	_	_	_	_	_	_	_	_	
$5.33\times10^{16}$	21.00	$1.60 \times 10^{27}$	7.68	$4.96 \times 10^{-27}$	$2.40 \times 10^{-25}$	$5.89 \times 10^{-31}$	1,200	581	
$6.40 \times 10^{16}$	17.50	$1.92 \times 10^{27}$	6.40	$2.87 \times 10^{-27}$	$1.16 \times 10^{-25}$	$2.84 \times 10^{-31}$	1,000	484	
$7.47 \times 10^{16}$	15.00	$2.24 \times 10^{27}$	5.55	$1.88 \times 10^{-27}$	$5.38 \times 10^{-26}$	$1.53 \times 10^{-31}$	856	415	
$8.55 \times 10^{16}$	13.10	$2.56 \times 10^{27}$	4.80	$1.28 \times 10^{-27}$	$2.73 \times 10^{-26}$	$2.92 \times 10^{-32}$	750	363	
_	_		_	_	_	_	_	_	
$4.10 \times 10^{17**}$	2.73	$1.23 \times 10^{28}$	0	$1.09 \times 10^{-29}$	$1.07 \times 10^{-29}$	$1.68 \times 10^{-34}$	156	75.5	
* Cravitational collarse ** Present time									

Table 1: The numerical result obtained from Eq.(23) show that the expansion rate is c when the radius of the universe is  $R_G = 6.20 \times 10^{24} = 2$  Mps. Making use of this scale, the expansion rate progressively decreases up to the present value of 150 km·s<sup>-1</sup>·(2 Mps)<sup>-1</sup> or 75.5 km·s<sup>-1</sup>·Mps<sup>-1</sup>. By use of the Eqts. (17) and (34),  $\rho_b$  and  $\rho_V$  are obtained. Using the Eq.(38) or 1/H, time is accomplished, the  $\rho_{CMB}$  result from Eq. (32)

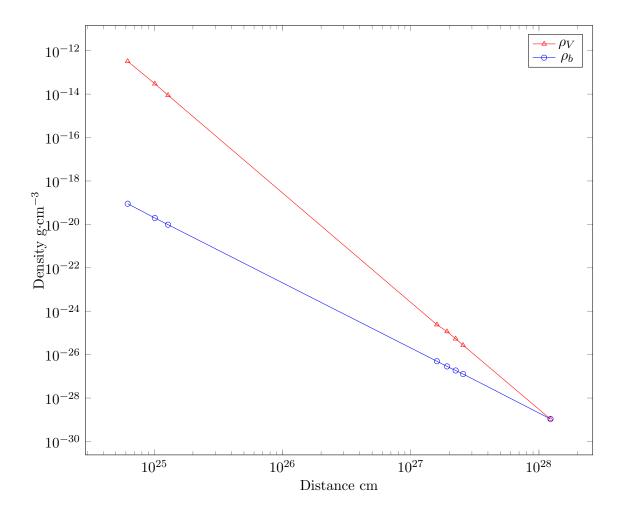


Figure 1: The red line represent the dynamical density of the vacuum  $\rho_V$ . The blue line represent the density of the baryonic matter  $\rho_b$ . The numerical values are from Table 1.

## 5 Cosmological time - temperature relationship

#### 5.1 Expansive ideal gas of photons

Since the whole cosmological space is a black body contour full of radiation and a very repulsive-expansive bubble of energy, the ideal gas equation as a kinetic expression is a suitable tool to resolve this problem directly.

$$V = \frac{N_{\gamma}kT}{\rho_{\gamma}c^2} \tag{36}$$

As the relation volume to radius is

$$R = \left(\frac{3}{4\pi}V\right)^{1/3}$$

Since  $t = \frac{R_U}{c}$ , substituting  $\rho_{\gamma}$  by Eq. (32), and dividing by c, we can determine the universe age in terms of the radiation temperature

$$t = \frac{\hbar}{kT} N_{\gamma}^{1/3} \tag{37}$$

If  $N_{\gamma} = 3.12 \times 10^{87}$  (Eq. 31), it means

$$T = 1.12 \times 10^{18} \,\mathrm{s} \cdot {}^{\circ}\mathrm{K} \cdot \mathrm{t}^{-1} \tag{38}$$

### 6 Formulation of the density of energy from the Casimir force

#### 6.1 Conversion of force into energy density

In the plane - plane geometry, the areas of both planes are  $L^2$ , and the pressure is independent of the extension of the areas. But in the sphere-plane geometry, when the radius of curvature is relatively high, (10 - 15 cm), this surface can be considered approximately as a plane. However the spherical surface causes an optical dispersion, which geometrically can be corrected by the factor  $2^3$ . Then, for the two system the Casimir pressure is expressed by

plane - plane sphere - plane 
$$\rho = \frac{\pi^2 \hbar c}{240 d^4} = 1.30 \times 10^{-18} \, \text{erg cm } d^{-4} \quad \rho = \frac{\pi^2 \hbar c}{120 d^4} = 2.60 \times 10^{-18} \, \text{erg cm } d^{-4}$$
 (39)

At the point of closest separations,  $d = 6.0 \times 10^{-5}$  cm, the static density of energy is  $0.20 \, erg \, cm^{-3}$ . For the micro electromechanical MEMS devices, the Casimir force and the Coulombic force are expressed by the following equation.

$$F_{Cas} = \frac{\pi^3 \hbar cR}{360 d^3} = 2.73 \times 10^{-20} \,\mathrm{dyn} \,\mathrm{cm}^3 \,d^{-3}$$
 (40)

$$F_{Coul} = \frac{\pi \varepsilon_0 RV^2}{d} = 5.15 \times 10^{-10} \,\mathrm{dyn} \,\mathrm{cm} \,d^{-1}$$
 (41)

Being  $R=0.01\,\mathrm{cm};\ \varepsilon_0=7.97\times 10^{-2}$  (dimensionless in cgs); V=0.136V (1 $V=3.333\times 10^{-3}\,\mathrm{cm}^{1/2}\,\mathrm{g}^{1/2}\,\mathrm{s}^{-1}$ )

In all microelectromecanics systems (Chan and similar) at the "point of closest approach"  $(7.6 \times 10^{-6} \, \text{cm})$  the Casimir force ( $\sim 7.0 \times 10^{-5} \, \text{dyn}$ ) is equal to the Coulombic force at 136 mV. This point, marks a limit, due to the fact that in all experiments a constant is obtained when the different results are derived in the form of energy density. Then, we can infer that all these "coincident" results, obeys the fact that are measurements of a constant of nature (Table 2).

The Casimir energy density within the boundaries of any microscopic cavity appears from an initially attractive interaction, which then, at the point of closest separation begins to have a repulsive perturbation. Reaching this balance, allows us to register the *static* energy density.

If we consider in Eqts. (40) and (41) as  $2R^2$  to be the effective area of the sphere, the static Casimir and the Coulombic pressure are:

$$\rho_{Cas} = \frac{\pi^3 \hbar c}{720 R d^3} = 1.36 \times 10^{-16} \,\text{erg } d^{-3} \tag{42}$$

$$\rho_{Coul} = \frac{\pi \varepsilon_0 V^2}{2Rd} = 2.57 \times 10^{-6} \,\mathrm{dyn} \,\mathrm{cm}^{-1} \,d^{-1} \tag{43}$$

e.g  $d = 7.57 \times 10^{-6}$ cm;  $\rho_{Cas} = 0.314 \, \text{erg cm}^{-3}$ ;  $\rho_{Coul} = 0.337 \, \text{erg cm}^{-3}$ 

 $<sup>^3</sup>$  The ratio between hemisphere surface / circle surface=  $\frac{2\pi R^2}{\pi R^2}=2$ 

Reference	Geometry	Sphere radius	Closest sep	Static Ener. Dens.	Dynamic dens.
		$\mathrm{cm}$	$\mathrm{cm}$	$\rho_{S_t} {\rm erg} {\rm cm}^{-3}$	$ ho_{\Lambda}~{ m g}~{ m cm}^{-3}$
Sparnaay; 1958	plane - plane	_	$\sim 5.0 \times 10^{-5}$	~0.21	$\sim 7.42 \times 10^{-30}$
Lamoreaux; 1997	plane - sphere	11.5	$6.0 \times 10^{-5}$	0.20	$7.06 \times 10^{-30}$
Roy - Mohideen; 1999	plane - sphere	0.01	$6.5 \times 10^{-6}$	0.50	$1.77 \times 10^{-29}$
Chan; 2001	plane - sphere	0.01	$7.6 \times 10^{-6}$	0.31	$1.10 \times 10^{-29}$
Bressi; 2002	plane - plane	_	$5.0\times10^{-5}$	0.21	$7.42 \times 10^{-29}$
Lisanti; 2005	plane - sphere	0.01	$7.6 \times 10^{-6}$	0.31	$1.10 \times 10^{-29}$
Iannuzzi; 2007	plane - sphere	0.01	$7.0 \times 10^{-6}$	0.40	$1.40 \times 10^{-29}$
Capasso; 2007	plane - sphere	0.01	$7.5 \times 10^{-6}$	0.32	$1.13 \times 10^{-29}$
Kim; 2009	plane - sphere	15.1	$5.0 \times 10^{-5}$	0.41	$1.48 \times 10^{-29}$
Sushkov; 2011	plane - sphere	15.6	$7.0\times10^{-5}$	0.11	$3.90 \times 10^{-30}$
Average				0.297	$1.06 \times 10^{-29}$

Table 2: The results of static energy density  $\rho_{st}$  is obtained from Eqts. (39) and (42). The dynamic energy density  $\rho_{\Lambda}$  is obtained from Eqts. (48), (49) and (50)

The Casimir static experimental energy density coincident with the obtained from the theoretical equation (33)  $\rho_{vac} = 0.015 \text{ erg} \cdot \text{cm}^{-3} \cdot {}^{\circ}\text{K}^{-3} \cdot T^{3}$ . Also the density is:  $\rho_{V} = \frac{0.296 \text{ erg} \cdot \text{cm}^{-3}}{C^{2}} = 3.30 \times 10^{-22} g \cdot \text{cm}^{-3}$ 

$$\rho_V = \frac{0.296 \text{ erg \cdot cm}^{-3}}{C^2} = 3.30 \times 10^{-22} g \cdot \text{cm}^{-3}$$

Which is the same:

$$\rho_V = \frac{4M_{U\,vacuum}}{3\pi R_U^2} = 3.30 \times 10^{-22} g \cdot \text{cm}^{-3}$$
(44)

#### Cosmological H and HeI highly excited Rydberg atoms 7

#### Thermic equilibrium between the CMB radiation and the Rydberg atoms

The cosmological space, acts as an entity since it expands by itself as an active element (dark energy). This phenomenon becomes clear by stretching the  $N_{\gamma}$  photons of the CMB radiation which permeates the whole cosmological space in a homogeneous form.

The Coulombic energy that an electron is retained (at any quantum level) pertaining to an isolated Rydberg hydrogen (or HeI) atom, is equivalent to the energy density of its empty surrounding contour. Despite of the obviousness of this assertion, if we use these atoms as cosmological micro barometers, we can make a measurement of the energy density of the empty space in all epoch. This measurement, can be performed from the inverse recombination (5,400°K) to the present time (2.73°K). In galaxies, intergalactic and in the intercluster medium, the undetectable dark matter, is formed by highly excited H Rydberg atom at n=220; Z=1, and for HeI; Z=1.34 at n=242, which its density is the same as the static density of energy of the cosmological empty space. Hence, the static density of energy of 0.75H and 0.25HeI are:

$$\rho_{240-220} = \frac{3Z^2 e^2}{8\pi n^6 a_0^4} = Z^2 3.51 \times 10^{13} \text{erg cm}^{-3} n^{-6}$$
(45)

Being:  $a_0$ : Bohr radius =  $0.529 \times 10^{-8}$ cm;  $e = 4.8 \times 10^{-10}$  cm<sup>3/2</sup> g<sup>1/2</sup> s<sup>-1</sup>

#### 7.2 Dynamic expression form of the energy density

The transition from the radiative era, to the gravitational era, occurs after the baryonic mass surpasses the mass-energy of the radiation at 5,400°K. At this epoch, the first clumps were formed and this point marks the initial time of the Hubble parameter. From Eq. (23) the radio between the Hubble constant at the present time, with respect its value at the gravitational collapse and other directly related parameters are equal to

$$Y_D^2 = \frac{H_0^2}{2H^2} = \frac{v^2}{2c^2} = \frac{T_{CMB}^2}{8T_G^2} = \frac{R_G^2}{8R_U^2} = \frac{1}{8(z+1)^2}$$

This index, defines the dynamic relativistic factor of the empty space in expansion. At present time  $Y_D^2$  is

$$Y_D^2 = \frac{1}{2} \left( \frac{75.4 \text{km s}^{-1} \text{Mps}^{-1}}{c \text{ km s}^{-1} \text{Mps}^{-1}} \right)^2 = \frac{1}{8} \left( \frac{2.73^{\circ} \text{K}}{5,400^{\circ} \text{K}} \right)^2 = \frac{1}{8} \left( \frac{6.4 \times 10^{24} \text{cm}}{1.23 \times 10^{28} \text{cm}} \right)^2 = \frac{1}{2} \frac{v^2}{c^2} = 3.18 \times 10^{-8}$$
(46)

# 7.3 Expression of the dynamic density for the Rydberg atoms and Casimir experimental results

The H and HeI atoms, which form the dark matter, behave as micro-barometers in hydrostatic equilibrium with the empty cosmological space. Likewise, these atoms are in thermodynamic equilibrium with the CMB radiation. In consequence of this physical subjections, the dynamical density of these Rydberg atoms is;

$$\rho_{Ryd} = \frac{3Z^2 e^2 Y_D^2}{8\pi a_0^4 c^2 n^6} = Z^2 1.25 \times 10^{-15} \text{ g cm}^{-3} n^{-6}$$
(47)

At present time  $Y_D{}^2 = 3.18 \times 10^{-8}$ ;  $Z^2 = 1$ ; n = 220;  $\rho_{Ryd} = 1.09 \times 10^{-29} \mathrm{g \, cm^{-3}}$ 

In the same way, the dynamic empty space density registered by the Casimir system is:

plane - plane

$$\rho_{Cas} = \frac{\pi^2 \, \hbar \, Y_D^2}{240 \, c \, d^4} = 4.62 \times 10^{-47} \, \text{g cm } d^{-4}$$
(48)

For  $d = 5 \times 10^{-5} \text{cm}$   $\rho_{Cas} = 7.40 \times 10^{-29} \text{g cm}^{-3}$ 

sphere - plane

$$\rho_{Cas} = \frac{\pi^2 \, \hbar \, Y_D^2}{120 \, c \, d^4} = 9.21 \times 10^{-47} \, \text{g cm } d^{-4}$$
(49)

For  $d = 5 \times 10^{-5} \text{cm}$   $\rho_{Cas} = 1.50 \times 10^{-29} \, \text{g cm}^{-3}$ 

MEMS microsphere - plane

$$\rho_{Cas} = \frac{\pi^3 \, \hbar \, Y_D^2}{720 \, R \, c \, d^3} = 4.82 \times 10^{-45} \, \text{g} \, d^{-3}$$
 (50)

For  $d = 7.6 \times 10^{-6} \text{cm}$   $\rho_{Cas} = 1.10 \times 10^{-29} \, \text{g cm}^{-3}$ 

In resume: the universe is formed by 0.005 of visible matter, 0.40 "dark" matter or Rydberg  $H - H_e$  atoms and 0.55 of "dark" energy. The "dark" energy was originated at the very beginning of the big bang process during the annhilation of near the same amount of matter - antimatter particles. This "dark" energy is the self energy of all the cosmological space in expansion (Secc. 4.3)

#### 8 Conclusions

In natural science, particularly in any branch of the physics, it is extremely hard to construct a scientific framework on basis of generalized hypothetical and enigmatic unknown forms of matter energy. Hence, it is very unusual, as in the cosmological "standard model", it is considered as a natural fact, that  $\sim 95\%$  of the matter-energy (near the whole) is in unknown hidden form.

Cosmology requires particles, radiation, space and energy; likewise, atomic physics and astrophysics require the same components. Since atomic physics and astrophysics do not make use of any hidden form of matter-energy, the theoretical cosmology must be free of these artifices. Given these failures, another physics, independent of the dogmas by the hegemonic standard model, would be essential and imperative. In this respect, a new interpretation of the experimental results of the Casimir effect, is a proof of this.

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