Some Relations Between Physical Constants

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Most of the following numerical relationships were found by me in the year 1991, while a few in 1994. I leave registered here to make it easier to return to the theme of Eletrogravitational Unification at most favorable time, with some of these relationships in mind (some = are probably \approx). Meanwhile, I leave it available to the public, if it is useful. The units were omitted in most case. Some corrections made in 2017.

1.
$$\frac{Ke}{G} \approx \frac{151}{7}$$

2.
$$KG \approx \frac{3}{5}$$

3.
$$\frac{1}{KG} \approx 1 + 10^{10} G$$

4.
$$\frac{1}{Gc} \approx 50$$

5.
$$\frac{K}{c} \approx 30$$

(obtained by 2. and 4.)

(this is a definition)

6.
$$\frac{\sqrt{e}}{G} \approx 6$$

7.
$$\frac{uec}{G} \approx \frac{151}{21} \approx \frac{Ke}{3G}$$

8.
$$uec = 10 c e \approx \frac{Ke}{3}$$

(charge of electron in e.s.u. or statC)

9.
$$\frac{K}{c^2} = 10^{-7}$$

10.
$$\frac{m_p c^2}{2} \approx 1.12 \ G \approx \frac{\sqrt{5}}{2} G$$

11.
$$\frac{8\pi}{c^3} \approx 557 \ m_n$$

12.
$$\frac{m_e c^2}{2} \frac{G}{Kh} \approx 0.5$$

13.
$$\frac{h}{k_{Boltz}} \approx (\sqrt{3} - 1) G$$

14.
$$\frac{m_p c^2}{2}/r_B \approx \sqrt{2}$$

15.
$$\frac{G}{h} = \frac{A}{6}$$

16.
$$\frac{\hbar}{2m_p} \approx \pi \cdot 10^{-8}$$

17.
$$Gm_p \approx 2Ke^2\delta$$
, $\delta = 4.57 r_B$

18.
$$\left(\frac{m_e}{m_p}\right)^3 \approx 3 \, r_B$$

19. $E_{gr} \approx F_{el} \, \delta, \, \delta = 9.14 \, r_B$ (equivalent to 17.)

20. $\frac{Gm_p^2}{r} = \frac{5h^3}{2m_p r^2}, \, r = 10^{-11} \, m$

$$\Rightarrow G = \frac{5h^3}{2m_p^3 r}$$

21. $\frac{Grav}{Weak} \approx \frac{2}{3} m_e \, (Grav: 0.6 \times 10^{-36}, \, Weak: 0.1 \times 10^{-5})$

22. $\frac{Grav}{Eletr} \approx \frac{h}{8} \, (Eletr: \frac{1}{137} \approx 0.0073)$

23. $\frac{m_p}{m_{Earth}} \approx \frac{1}{4} \, h^{3/2}$

24. $F_{Earth-Sun} \approx 5 \, h^{-1.3}$

25. $Ke^2 \approx 5 \, (Gm_p)^{3/4}$

26. $\frac{1}{2} mv^2 \approx \frac{Ke^2}{r}$

27. $m_p + \frac{m_e}{\sqrt{1-\frac{v^2}{c^2}}} = m_n$

28. $m_p \, c \approx 3 \, e$

29. $\frac{8\pi^2}{\mu_0} \approx \frac{c}{4} = \left(\frac{m_e}{h}\right)^2$ (instead of 8 a better value is 9.5)

30. $\frac{h^2}{2m} \nabla^2 \Psi + (E - V)\Psi = 0$

$$\Rightarrow \nabla^2 \Psi + \frac{c}{4} v^2 \Psi = 0 \, (m = m_e)$$

Another relationship, which most calls my attention, refers to the difference between the charge of the electron and the proton, based on an old theory of Eletrogravitational Unification that I created^[1], is as follows:

$$e - p \approx 8.376 \times 10^{-55}$$

$$\frac{e - p}{e} \approx 5.228 \times 10^{-36}; \ h = 6.6260754 \times 10^{-34};$$

$$\frac{e - p}{e} \cdot \frac{1}{h} \approx 0.00789 = 7.89 \times 10^{-3} \approx \frac{1}{126.742} \approx \frac{1}{127} \approx \alpha,$$

where α is the fine-structure constant:

$$\alpha = \frac{1}{4\pi\varepsilon_0} \frac{e^2}{\hbar c} = \frac{\mu_0}{4\pi} \frac{e^2}{\hbar c} = K \frac{e^2}{\hbar c} = \frac{1}{2\varepsilon_0} \frac{e^2}{\hbar c} \approx 7.29735 \times 10^{-3} \approx \frac{1}{137.036}.$$

The recommended values of these constants you may see in [2] or [3].

Reference

- 1. Godoi, Valdir M. S., *A Unificação Eletrogravitacional do Ponto de Vista Clássico*, Boletim do Instituto de Matemática e Física da Universidade Federal de Goiás, nº 15, ano 7, novembro (1992). Available in http://gsjournal.net/Science-Journals/%7B\$cat name%7D/View/5690 (2015) and http://www.vixra.org/abs/1407.0192 (2014).
- 2. Peter J. Mohr, David B. Newell, Barry N. Taylor, CODATA Recommended Values of the Fundamental Physical Constants: 2014, available in https://arxiv.org/pdf/1507.07956.pdf (2015).
- 3. https://physics.nist.gov/cuu/Constants/index.html.